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The Evolution of U.S. Retail Concentration

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Abstract

Increases in concentration have been a salient feature of industry dynamics during the past 30 years. This trend is particularly notable in the U.S. retail sector, where large national firms have displaced small local firms. Existing work focuses on national trends, yet less is known about the dynamics of concentration in *local* markets and the relationship between local and national trends. We address these issues by providing a novel decomposition of the national Herfindahl-Hirschman Index into a local and a cross-market component. We measure concentration using new data on product-level revenue for all U.S. retail stores and find that despite local concentration increasing by 34 percent between 1992 and 2012, the cross-market component explains 99 percent of the rise in national concentration, reflecting the expansion of multi-market firms. We estimate an oligopoly model of retail competition and find that the increase in markups implied by rising local concentration had a modest effect on retail prices. JEL: L8

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1 Introduction

In the past 30 years, U.S. retailing has become substantially more concentrated. Between 1997 and 2007, the share of sales going to the 20 largest firms increased from 18.5 percent to 25.4 percent (Hortaçsu and Syverson, 2015) and the national Herfindahl-Hirschman Index (HHI) in retail doubled. These patterns appear to be part of an economy-wide trend toward greater ownership concentration (Autor, Dorn, Katz, Patterson, and Van Reenen, 2020) and an increase in the dominance of large, established firms (Decker, Haltiwanger, Jarmin, and Miranda, 2014). There is also evidence that increases in concentration are accompanied by steeply rising variable markups (De Loecker, Eeckhout, and Unger, 2020; Hall, 2018), which raises concerns about rising market power.

These findings rely on national industry-based evidence. However, local product-based concentration is more informative than national industry-based concentration about the degree of competition and the evolution of markups in retail, because consumers in the retail sector primarily choose between local stores selling a given product. Thus, to understand the evolution of concentration in the retail sector we construct a new product-based measure of local concentration by assembling data on sales by product category for all U.S. retail establishments. We also assess the relationship between local concentration and the observed trends in national concentration.

The relationship between trends in local and national concentration is not ex-ante clear. Growth in national concentration may not imply increasing local concentration. To see this, suppose that each U.S. city starts with a different largest store. If a national retailer replaces the largest store in each market, without displacing any business from the smaller stores, then national concentration would rise, while local concentration would not. Alternatively, growth in national retailers might displace not just the largest stores but also smaller local ones, in which case growth in national concentration would be accompanied by growth in local concentration. Whether the national expansion of large retailers, such as Walmart and Target, increases local retail concentration depends on whether they displace large-, medium-, or small-sized local retailers.¹

To determine the relationship between the trends of local and national concentration, we develop a novel decomposition of the national HHI into a component driven by local market concentration and a new component that we call "cross-market" concentration, which is driven by consumers in different markets shopping at the same firms. The decomposition exploits a new interpretation of the HHI as the probability that two dollars spent at random in a market are spent in the same firm. We use this decomposition to separate the contribution of changes in local markets to national concentration from the contribution of the expansion of retail chains that occurred since the 1990s.

We implement our decomposition and provide new measures of product-level local concentration using new data on store-level revenue for all U.S. retailers in eight major categories of goods between 1992 and 2012. We combine two sources of confidential U.S. Census Bureau microdata, namely the Census of Retail Trade (CRT) and the Longitudinal Business Database (LBD). The coverage of the data allows us to document the evolution of U.S. retail concentration at the local level.

These new data also allow us to improve over previous measures of retail concentration that rely on industry-based classifications of retail markets.² Industry-based measures do not account for the increasing importance of multi-product retailers (such as general merchandisers and non-store retailers like e-commerce merchants) that compete across various industries. For example, Walmart is in the general merchandising subsector (3digit NAICS 452) but competes with grocery, clothing, and toy stores.³ In fact, general merchandisers account for more than 20 percent of sales in Electronics and Appliances, Groceries, and Clothing, demonstrating that competition across industries is a relevant feature of retail markets.

¹References to specific firms are based on public data and do not imply the company is present in the confidential microdata.

 $^{^{2}}$ In Appendix E we document differences between industry- and product-based measures of concentration. These measures are conceptually different, as they have different definitions of a market.

³Walmart reports SIC code 5331 to the Security and Exchange Commission, which corresponds to NAICS 452319 (Securities and Exchange Commission, 2020).

Using these data, we document three new facts on concentration in the retail sector. First, we show that both the national and local HHI increase, but at different rates, with the national HHI increasing faster than the local HHI. Second, the decomposition of national HHI shows that 99 percent of the change in national concentration is driven by consumers in different markets shopping at the same firms (cross-market concentration), with less than 1 percent driven by changes in local concentration. Cross-market concentration, which measures the probability that two dollars spent in the same product category are spent at the same firm in two different markets, increased more than threefold, from around 1.2 percent to 4.2 percent between 1992 and 2012. Local concentration, which measures the probability that two dollars spent in the same market are spent at the same firm, increased by 34 percent, from 6.4 percent to 8.5 percent. Third, we show that the majority of markets and product categories feature increasing concentration. The local HHI increased in 57 percent of commuting zones accounting for 59 percent of retail sales between 2002 and 2012; the increases were even larger in the previous decade, with 70 percent of commuting zones (accounting for 73 percent of retail sales) increasing their concentration between 1992 and 2002. The local HHI also increased for seven of the eight major product categories in retail between 1992 and 2012, with Clothing being the exception.

We focus on concentration among brick-and-mortar stores, which account for most of the retail sector sales between 1992 and 2012. While online and other non-store retailers have increased in importance, they account for less than 10 percent of retail sales in 2012 and hence have a small effect over the level of local concentration. We show that under plausible assumptions over how non-store retailers sales are distributed across markets, the introduction of their sales is likely to decrease local concentration, especially for products like electronics or sporting goods, where their market share is highest.

The broad increase in local concentration implies that market power could help explain rising markups in the retail sector, which can potentially harm consumers. Studying the historic relationship between concentration and markups is challenging because long series on prices and costs for U.S. retailers are not available. Thus, we estimate a model of local retail competition based on the work of Atkeson and Burstein (2008). The model features strong parametric assumptions that make it tractable enough to derive an explicit link between the local HHI and average markups at the product level. We exploit this link to estimate the model with available data. We find that increasing local concentration raised markups by 2 percentage points in the retail sector between 1992 and 2012, a third of the increase found in the Annual Retail Trade Survey (ARTS).

The increase in markups is small relative to the 34 percent decrease in retail prices observed in the same period. Lower prices may be due to low-cost firms increasing their market share, which increases concentration but has an ambiguous effect on welfare, making it difficult to conclude the effect on consumers (Bresnahan, 1989). But even if lower costs could have been achieved without increased local concentration, an unlikely scenario, prices would have fallen only 1 percentage point more over 20 years, implying a limited effect of concentration on consumers.

Our main contribution comes from distinguishing between local and national concentration by providing new direct measures of local retail concentration. Higher national concentration has been related to the decline in the labor share (Autor et al., 2020), the decline of churn and reallocation of aggregate activity to large established firms (Decker et al., 2014, 2020), lower long-term growth due to lower innovation as competition decreases (Aghion, Bergeaud, Boppart, Klenow, and Li, 2019), and concerns about market power and rising markups (De Loecker et al., 2020; Hall, 2018; Edmond et al., 2019; Traina, 2018). However, many of these concerns would operate through local markets, particularly in labor and retail markets. Higher local employment concentration has been shown to negatively impact wages (Berger, Herkenhoff, and Mongey, 2019; Jarosch, Nimczik, and Sorkin, 2020; Azar, Berry, and Marinescu, 2019; Rinz, 2020). We focus on retail product markets where sales are overwhelmingly local and explicitly show that changes in national concentration are due to the expansion of multi-market firms and

are not informative about changes in local retail concentration. Our results show local concentration is increasing across most markets and products but that these changes imply only modest increases in markups.

The closest paper to ours is Rossi-Hansberg, Sarte, and Trachter (2020), which evaluates changes in concentration at both the national and local levels in multiple sectors (e.g., manufacturing, retail) using the U.S. National Establishment Time Series (NETS) establishment-level data set. They find that between 1992 and 2012, concentration at the national level increased in six major sectors, while local concentration decreased.⁴ Our findings at the national level are similar to those in Rossi-Hansberg et al. (2020). However, our results at the local level differ sharply, as we find significant increases in local concentration for most product categories.⁵ There are multiple reasons for our results to differ, but one major reason is that different data are used. The data we use are based on confidential information collected by the Census Bureau and the Internal Revenue Service (IRS), and they are considered the gold standard for measuring economic activity at the store level. These records make it clear that local concentration in retail has been increasing, though not as much as national concentration. We discuss this further in Appendix A.

We also contribute to substantial work documenting changes in the structure of the retail sector. Our paper clearly shows that national concentration does not reflect trends in local concentration. Instead, increasing national concentration reflects consumers in different markets shopping at the same firms. Thus, we help highlight the role of the expansion of large firms in explaining changes in the U.S. firm size distribution (Cao, Hyatt, Mukoyama, and Sager, 2019; Hsieh and Rossi-Hansberg, 2019). These large retail firms, particularly Walmart and Target, have been shown to lead to the closing of small

⁴For the retail sector, national concentration increased by 5 percentage points, while local level concentration decreased by 14 percentage points. Numbers are taken from the retail sector line in Figure 2 in Rossi-Hansberg et al. (2020).

⁵These results are in line with other studies documenting that local trends in retail may differ from local trends in other sectors. Rinz (2020) and Lipsius (2018) find increasing labor market concentration in retail, but find decreasing labor market concentration overall using the LBD.

stores (Jia, 2008; Haltiwanger, Jarmin, and Krizan, 2010), grocery chains (Arcidiacono, Bayer, Blevins, and Ellickson, 2016), and lower retail employment in local labor markets (Basker, 2005). Additionally, we measure national and local concentration using productlevel revenue, which handles the multi-product nature of large retailers. This complements previous work that has found increasing national retail concentration at the industry level (Foster, Haltiwanger, Klimek, Krizan, and Ohlmacher, 2016; Hortaçsu and Syverson, 2015; Grullon, Larkin, and Michaely, 2019; Autor et al., 2020).

The rest of the paper proceeds as follows. Section 2 develops a decomposition of national concentration into local and cross-market concentration. Section 3 describes the data, including how we construct store-level sales by product. Section 4 measures national and local concentration and establishes the main facts about their evolution since 1982. Section 5 discusses the effects of local concentration on markups. Section 6 concludes.

2 National and Local Concentration

The increasing trend of national concentration in various sectors of the economy has been widely documented (Autor et al., 2020; Decker et al., 2020; Akcigit and Ates, 2021; Aghion et al., 2019; Hsieh and Rossi-Hansberg, 2019). However, local concentration is the relevant measure of concentration for competition in the retail sector, as consumers typically shop at nearby stores (Rossi-Hansberg et al., 2020). One major outstanding question concerns what we can learn about local concentration from the change in national concentration.

Increasing national concentration can be accompanied by increasing local concentration, but it may also be accompanied by decreases in local concentration. In fact, not much can be learned from the dynamics of local concentration if we only have information about national trends. The simple example shown in Figure 1 makes this clear. National concentration can increase by having firms expand across markets, without affecting the layout of individual markets (row 2). Alternatively, the expansion of large firms can drive out competitors in

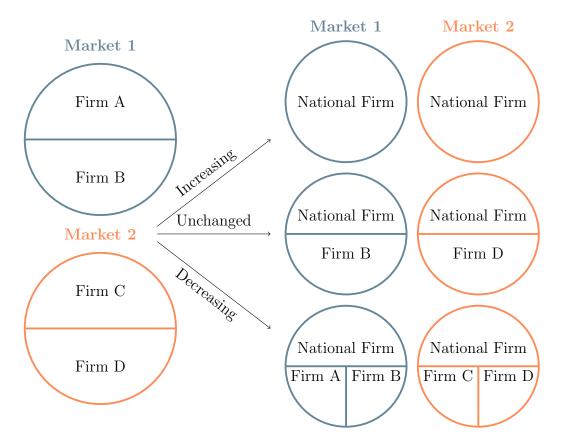


Figure 1: Effect of Increasing National Concentration on Local Concentration

Notes: The figure shows hypothetical market structures after the entry of a national firm in a two market economy that starts with four local firms.

local markets, increasing national and local concentration (row 1), or it can bring up more and likely smaller—competitors, decreasing local concentration (row 3). The total effect on national and local concentration depends on how firms in individual markets respond.

The example in Figure 1 highlights the two mechanisms affecting national concentration that we study in this paper: changes in local concentration and changes in cross-market concentration. The first mechanism links changes in the composition of local markets and concentration at the national level. As local markets become more/less concentrated, so does the aggregate economy (in a given sector). The second mechanism links national concentration to the presence of multi-market firms. As firms expand across markets, they capture a larger share of national sales, in turn increasing national concentration. Note that, as shown in Figure 1, changes in cross-market concentration need not be accompanied by changes in local concentration. In what follows we make these ideas precise by developing a new decomposition of national concentration into local and cross-market concentration.

Our primary measure of concentration is the firm Herfindahl-Hirschman Index (HHI). The HHI is one of the most common measures of concentration, and its formulation will prove useful in decomposing the mechanisms behind the changes in national concentration. We measure concentration at the product category level. We denote by i an individual firm and by j a product, so that s_i^{jt} represents the sales share of firm i in product j at time t. More generally, we define subscripts and superscripts such that s_a^b is the share OF a IN b. The national HHI in a year is defined as the sum of the product-level HHIs, weighted by the share of product j's sales in total retail sales, s_i^t :

$$HHI^{t} = \sum_{j=1}^{J} s_{j}^{t} HHI_{j}^{t}, \quad \text{with} \quad HHI_{j}^{t} = \sum_{i=1}^{N} \left(s_{i}^{jt}\right)^{2}, \tag{1}$$

while the HHI of location ℓ and product j in year t is calculated as

$$HHI_{\ell j}^{t} = \sum_{i=1}^{N} \left(s_{i}^{j\ell t} \right)^{2}.$$
(2)

From equation (1), it is clear that the national HHI for product j measures the probability that two dollars, x and y, chosen at random, are spent at the same firm.⁶ We use the law of total probability to derive a decomposition of the HHI into two terms, based on whether the two dollars are spent in the same or different markets. The decomposition is given by

$$\underbrace{P(i_x = i_y)}_{\text{National HHI}} = \underbrace{P(\ell_x = \ell_y)}_{\text{Local HHI}} \underbrace{P(i_x = i_y | \ell_x = \ell_y)}_{\text{Local HHI}} + \underbrace{P(\ell_x \neq \ell_y)}_{\text{Cross-Market HHI}} \underbrace{P(i_x = i_y | \ell_x \neq \ell_y)}_{\text{Cross-Market HHI}}, \quad (3)$$

⁶In what follows, the *j* and *t* superscripts are dropped on all variables for convenience. In this context a market is characterized by its location, ℓ , as the product is fixed.

where i_x is the firm at which dollar x is spent and ℓ_x is the location of the market in which dollar x is spent, and likewise for y.

Equation (3) has three components. The first component, $P(\ell_x = \ell_y)$, which we term collocation, captures the probability that two dollars are spent in the same location.⁷ The second component, $P(i_x = i_y | \ell_x = \ell_y)$, is an aggregate index of local concentration, with local concentration measured as in equation (2).⁸ This captures the extent to which consumers in a local market shop at the same firm. The third component, $P(i_x = i_y | \ell_x \neq \ell_y)$, which we call cross-market concentration, captures the probability that a dollar spent in different markets is spent at the same firm:

$$P(i_x = i_y | \ell_x \neq \ell_y) = \underbrace{\sum_{\ell} \sum_{n \neq \ell} \frac{s_\ell s_n}{1 - \sum_p s_p^2}}_{\text{Weights}} \underbrace{\sum_{i=1}^N s_i^\ell s_i^n}_{\text{Cross-Market}} .$$
(4)

The cross-market concentration index between two markets (say ℓ and n) is given by the product of the shares of the firms in each location (the probability that two dollars spent one in each location are spent in the same firm). The pairs of markets are then weighted by their share of sales and are summed.

Of the three terms, the collocation term plays a crucial role in determining the impact of local concentration in national measures. A low collocation term implies that local concentration can only have a limited effect on national trends, leaving the cross-market term as the driver of the national index. We will show later that this is in fact the case, which should come as no surprise because the U.S. has many markets and even the largest markets represent only a small fraction of total U.S. sales.

To implement the decomposition presented in equation (3), we need to measure

⁷The collocation term is $P(\ell_x = \ell_y) = \sum_{\ell=1}^{L} (s_\ell)^2$, where s_ℓ is the share of location ℓ in national sales. ⁸In the decomposition each local market is weighted by the conditional probability that the two dollars are spent in location ℓ given that they are spent in the same location: $s_\ell^2/(1-\sum_p s_p^2)$. These weights give more importance to larger markets than the more usual weights s_ℓ —the share of sales (of product j) accounted for by location ℓ (at time t). We present aggregated series for local concentration in Section 4 that use the latter weights. Appendix B derives these results in detail.

concentration in each local market for a given product as well as link the activities of firms across markets. Doing this requires detailed data on establishment-level revenue by product for all firms in the U.S., which we describe in the next section.

3 Data: Retailer Revenue for All U.S. Stores

This section describes the creation of new data on store-level revenue for 18 product categories for all stores with at least one employee in the U.S. retail sector. These data allow us to construct detailed measures of concentration that take into account competition between stores selling similar products in specific geographical areas.⁹

3.1 Data Description

We use confidential U.S. Census Bureau microdata that cover 1992 to 2012 (Bureau of the Census, 1992-2012). The source of the data is the Census of Retail Trade (CRT), which provides revenue by product type for retail stores in years ending in 2 and 7. The CRT data on product-level revenue and information on each store's location are used to define which stores compete with each other. Importantly, a store's local competition will include stores in many different industries inside the retail sector because stores of different industries can sell similar products. This is particularly relevant for stores in the general merchandising subsector that sell multiple product types. The data we create here are uniquely equipped to deal with cross-industry competition. We combine the CRT data with the Longitudinal Business Database (LBD) (Jarmin and Miranda, 2002), which contains data on each store's employment and allows us to track stores over time.

 $^{^{9}\}mathrm{We}$ use store and establishment as synonyms.

3.2 Sample Construction

The retail sector is defined based on the North American Industrial Classification System (NAICS) as stores with a 2-digit code of 44 or 45. As such, it includes stores that sell final goods to consumers without performing any transformation of materials. From 1992 to 2012, we use the NAICS codes available from the CRT as the industry of each store. Prior to 1992, we use the store-level NAICS codes imputed by Fort and Klimek (2018). The sample includes all stores with positive sales and valid geographic information that appear in official CRT and County Business Patterns statistics that sell one of the product categories used in this study.¹⁰

Table 1 shows summary statistics for our sample. Even though the number of establishments and firms fluctuates over time, there is an overall decrease in both counts between 1992 and 2012. Notably, the decrease in firms is double that of establishments. This trend is consistent with the growing importance of multi-market firms in rising cross-market concentration that we show in Section 4. Despite these trends, employment increases over time, representing about 9 percent of U.S. employment over the whole sample period.¹¹

3.3 Creation of Product-Level Revenue

We construct product-level revenue data for all U.S. stores, allowing us to assign a store in a given location to markets based on the types of products it carries. To do this, we exploit the CRT's establishment-level data on revenue by product line (e.g., men's footwear, women's pants, diamond jewelry). We then aggregate product line codes into 18 categories such that stores in industries outside of general merchandise and non-store retailers sell

¹⁰We exclude sales of gasoline and other fuels, autos and automotive parts, and non-retail products because franchising makes it difficult to identify firms. In our main results we exclude non-store retailers because sales from these stores are typically shipped to different markets than their physical location. We explore the implications of this assumption in Section 4.4.

¹¹U.S. employment numbers come from Total Nonfarm Employees in the Current Employment Statistics (Bureau of Labor Statistics, 2019).

	1992	1997	2002	2007	2012
Establishments	908	942	913	912	877
Firms	593	605	589	566	523
Sales	$1,\!004$	1,368	$1,\!657$	2,062	$2,\!195$
Employment	9.91	11.60	11.89	12.78	12.31

 Table 1: Sample Summary Statistics

Notes: Establishment and firm numbers are expressed in thousands. Sales and employment numbers are expressed in millions. The numbers are based on calculations from the Census of Retail Trade and the Longitudinal Business Database.

primarily one type of product.¹² For instance, stores in industries beginning with 448 (clothing and clothing accessory stores) primarily report sales in products such as women's dress pants, men's suits, and footwear, which are grouped into a Clothing category.

Aggregating product lines into categories allows us to accurately impute revenue by category for stores that do not report product-level data. The CRT asks for sales by product lines from all stores of large firms and a sample of stores of small firms. For the remainder, store-level revenue estimates are constructed from administrative data using store characteristics (e.g., industry and multi-unit status), which affects stores that account for 20 percent of sales. Appendix C provides the details of this procedure.

Our product-level revenue data accounts for the presence of multi-product stores. When a store sells products in more than one category, we assign the store's sales in each category to its respective product market. Consequently, a given store faces competition from stores in other industries. For example, an identical box of cereal can be purchased from Walmart (NAICS 452), the local grocery store (NAICS 448), or online (NAICS 454).¹³

Table 2 shows that cross-industry competition is pervasive in retail. On average, the

¹²Table C.2 lists all the product categories. We will focus on the eight "main" product categories that account for about 82 percent of sales of the stores in our sample throughout the entire time period. The remaining categories are individually small and have not been released due to disclosure limitations.

¹³The authors found a 10.8 oz box of Honey Nut Cheerios at Walmart, Giant Eagle, and Amazon.com on June 22, 2020.

main subsector for each product accounts for just over half of the product's sales. The remaining sales are accounted for by multi-product stores, particularly from the general merchandise and non-store retailer industries, which are included in the appropriate product markets based on their reported sales. The high sales shares of these multi-product stores makes industry classifications problematic when studying competition. Table D.1 of Appendix D reports the composition of sales for each product retailers. Appendix E reports results by industry and compares them to our product measures. Industry-based concentration also increase at the national and local level, but the changes across products categories differ from the changes in their main subsector.

Table 2: Share of Product Category Sales by Main Subsector

	1992	2002	2012
Avg. Main Subsector Share	55.8	53.2	50.0
Max Main Subsector Share	79.8	73.1	72.4
Min Main Subsector Share	30.3	27.6	22.0

Notes: The numbers are based on calculations from the Census of Retail Trade. The average is the arithmetic mean across the eight main product categories of the share of sales accounted by establishments in the product's associated subsector.

4 Changes in Retail Concentration

In this section, we exploit the detailed microdata described in Section 3 to decompose national concentration in the U.S. retail sector into local and cross-market concentration, using the identity developed in equation (3). The measure of local concentration we compute accounts for the local nature of competition in retail and has a distinct advantage in that it measures concentration at the product category level, rather than the industry level, addressing the rise of general merchandisers that compete with stores across multiple industries.¹⁴ In what follows, we show that local concentration has increased, although not as much as national concentration. Moreover, the decomposition reveals that national concentration is largely independent of local trends, with over 99 percent of the growth in national concentration accounted for by increasing cross-market concentration (consumers shopping at the same firms across markets).

Figure 2 plots national concentration in the U.S. retail sector as measured by the HHI defined in equation (1). Between 1992 and 2012, national concentration more than tripled. The probability that two dollars are randomly spent in the same retail firm went from 1.3 percent to 4.3 percent. Most of this increase occurred between 1997 and 2007. In fact, the national HHI was low and grew at a low rate in the years before 1997. In Appendix D we extend our sample to 1982 and show that national concentration increased by 1 percentage point in the 15 years between 1982 and 1997; in contrast it increased 2.3 percentage points in the 10 years between 1997 and 2007. However, and despite the striking increase in national concentration, Figure 2 provides almost no information on the underlying changes in local retail markets.

Figure 3 plots the level of national and local concentration between 1992 and 2012. Local concentration increases whether markets are defined by zip codes, counties, or commuting zones. Between 1992 and 2012, three of the four measures increased by about 2 percentage points, with the commuting zone HHI increasing by 34 percent from 0.064 to 0.085. But contrary to the national concentration index, local concentration did not accelerate its increase in the period after 1997. When we extend these results back to 1982, we find no change in the trends for local concentration until 2007, when all concentration measures plateau (Appendix D).

The national concentration results are consistent with previous industry-level work using sales and employment for various sectors, including retail (Rossi-Hansberg et al., 2020; Autor et al., 2020; Foster et al., 2016; Basker et al., 2012; Lipsius, 2018; Rinz,

¹⁴We calculate all concentration measures at the firm level by combining sales of the stores of a firm in each market.

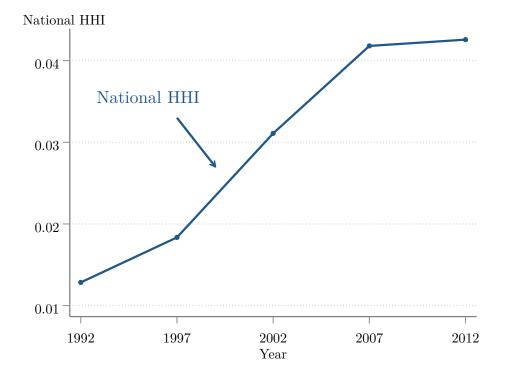


Figure 2: National Concentration

Notes: The numbers are based on calculations from the Census of Retail Trade. The numbers are sales weighted averages of the national Herfindahl-Hirschman Index (HHI) in eight main product categories.

2020). The local concentration results are also consistent with studies on local labor market concentration that find increasing concentration in retail but decreasing local concentration overall (Rinz, 2020; Lipsius, 2018). Our results suggest that increasing local retail concentration may help explain the increases in markups documented in De Loecker et al. (2020). We show in Section 5 that this is in fact the case, with local concentration implying modest increases in markups for all product categories.

However, the picture that emerges from our data differs from the findings at the local level of Rossi-Hansberg et al. (2020), who find that local retail concentration has been steadily falling since 1992. Our results differ for multiple reasons. First, we use a different data set.¹⁵ Second, different definitions of which stores are retailers are employed.

¹⁵Rossi-Hansberg et al. use U.S. National Establishment Time Series (NETS) data.

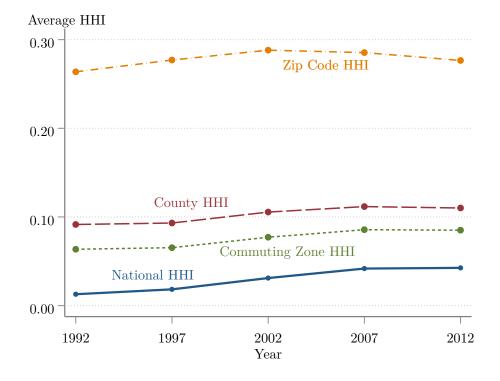


Figure 3: National and Local Concentration

Notes: The numbers are based on calculations from the Census of Retail Trade. The figure plots the Herfindahl-Hirschman Index (HHI) for three different geographic definitions of local markets and national concentration. The local HHI is aggregated using each location's share of national sales within a product category. The numbers are sales weighted averages of the corresponding HHI in eight main product categories.

Rossi-Hansberg et al. use Standard Industrial Classification (SIC) codes, while this paper uses NAICS.¹⁶ Finally, the aggregate index of local HHI is calculated differently. Rossi-Hansberg et al. report the average change in the local HHI, weighting by the end-of-period sales/employment of each market, while we report the change in the average local HHI, weighting markets in each year according to that year's sales. This distinction matters because as markets become bigger, they also tend to become less concentrated. This mechanically gives more weight to markets where concentration is decreasing. In fact, when we repeat our exercise using end-of-period weights, we find slight decreases in local concentration both at the industry and the product level. We

¹⁶The primary difference between SIC and NAICS is that SIC includes restaurants in retail.

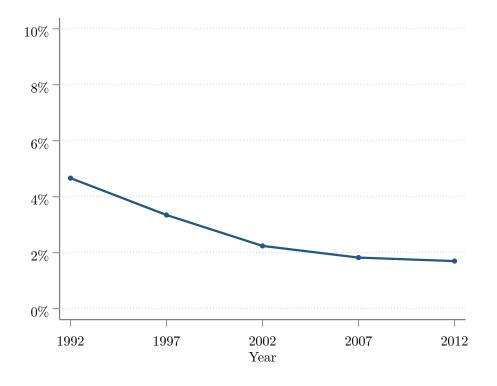


Figure 4: Share of Local Concentration Term in National Concentration

Notes: The numbers are based on calculations from the Census of Retail Trade. The share of local concentration is measured as the ratio of the local concentration term in equation (3) to the national Herfindahl-Hirschman Index (HHI). The local concentration term is the product of the collocation term and local HHI. We aggregate the local concentration terms across the eight main product categories using their sales shares.

choose current period weights so that we can decompose national concentration as described in Section 2. We expand upon differences between our studies in Appendix A.

4.1 Decomposing National Concentration

We now assess the contribution of local and cross-market concentration to national concentration, using the decomposition in equation (3). We focus on the 722 commuting zones that partition the contiguous U.S. as our definition of local markets in what follows. Commuting zones are defined by the U.S. Department of Agriculture such that the majority of individuals work and live inside the same one and provide a good

approximation for the retail markets in which stores compete.¹⁷ Choosing a larger geographical unit when defining retail markets decreases the level of local concentration and increases the contribution of local concentration to national concentration, relative to smaller geographical units like counties or zip codes.

Figure 4 shows the contribution of local concentration to national concentration by product category and year. Two things are clear. First, the contribution of local concentration to national concentration is small, never above 5 percent. This is because local concentration is weighted by the collocation term—the probability that two dollars spent in the U.S. are spent in the same market—which is small given the large number of markets in the country.¹⁸ Second, the contribution of local concentration has been falling over time as national concentration has been increasing. By 2012, local concentration accounted for just 1.7 percent of the level of national concentration.

The flip side of these results is the major role of cross-market concentration in shaping the national concentration index. National concentration has increased because consumers in different locations are shopping at the same (large) firms; in fact, 99 percent of the change in national concentration is accounted for by changes in cross-market concentration.

4.2 Changes in Concentration across Markets

The increases in concentration have been broad based. Almost 60 percent of dollars spent in 2012 are spent in markets that have increased concentration since 2002. Figures 5b and 5d show the distribution of changes in concentration between 2002 and 2012. In just 10 years, 23 percent of markets had increases in concentration of over 5 percentage points. These changes are significant. One criterion used by the Department of Justice to determine

¹⁷It seems likely that if individuals live and work in a commuting zone, they do the majority of their shopping in that region. Calculating results in this way causes us to potentially overstate the role of local concentration in national trends relative to using smaller geographic units.

¹⁸The collocation term is stable across time and is always less than 2 percent. See Appendix D.

when to challenge mergers is whether the local HHI will increase by 2 percentage points (Department of Justice and Federal Trade Commission, 2010).

The increases in local concentration were even more widespread in the decade from 1992 to 2002. Over 69 percent of markets accounting for 72 percent of retail sales increased their concentration. Figures 5a and 5c show the distribution of changes in concentration during this time period. Most of the retail sales are concentrated in markets with relatively small increases in concentration (between 0 and 5 percentages point increases in the market's HHI), both in the 1992–2002 decade and the 2002–2012 decade. These markets account for 66 percent of retail sales in 2002 and for 55 percent in 2012.

4.3 Changes in Concentration across Products

Both local and national concentration increased for seven of the eight major product categories between 1992 and 2012, clothing being the exception. Figure 6 shows that these increases were significant for many products. Six of the eight categories had an increase in HHI between 3 and 4 percentage points, even though in 1992 the average level of the local HHI was relatively low; only Toys was above 0.1. Despite this common trend, there is substantial variation across product categories in the changes in concentration. Local concentration in Groceries increased by only 1.1 percentage points, and it actually decreased in clothing by 2012, while it almost doubled in Home Goods and Electronics and Appliances. However, six of the categories experienced larger absolute changes in national and cross-market concentration even though the levels of national and cross-market concentration are markedly lower than those of local concentration.

Figures 7a and 7b show results for national and cross-market concentration and make clear the tight link between these indexes. Both measures show the same patterns, differing only in the third decimal due to changes in local concentration. The limited impact of local concentration is due to the nature of the collocation term of equation (3), which is remarkably small and constant across products and time (see Appendix D).

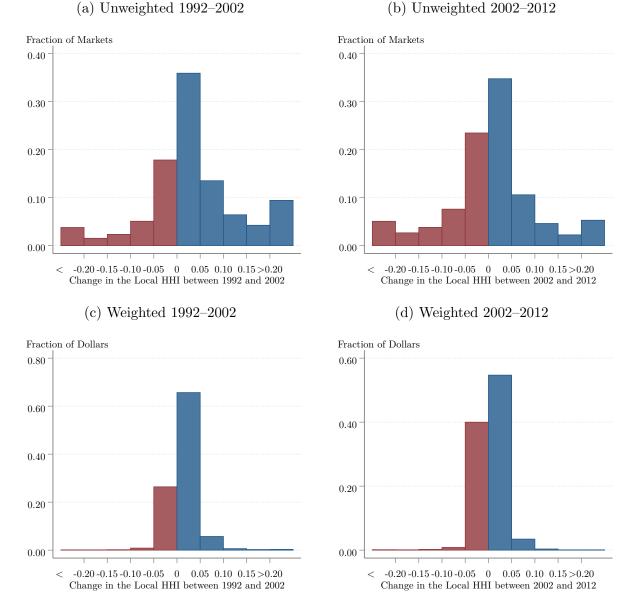


Figure 5: Changes in Concentration across Markets

Notes: The numbers are based on calculations from the Census of Retail Trade. The top panels show the fraction of markets, commuting zone/product category pairs, with changes in concentration of a given size. The bottom panels weight markets by the value of sales in the product category. The columns report changes for the decades 1992 to 2002 and 2002 to 2012.

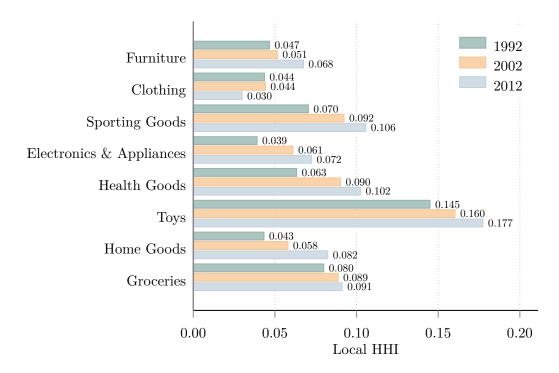


Figure 6: Local Concentration across Product Categories

Notes: The numbers are local Herfindahl-Hirschman Indexes (HHI) by product weighted by market size from the Census of Retail Trade microdata.

Finally, comparing Figures 6 and 7 shows that not all product markets evolved in the same way between 1992 and 2012. The markets for Furniture and Clothing changed very little, and both have relatively low levels of both local and national concentration. On the other hand, local markets for Groceries and Health Goods have become slightly more concentrated, while at the national level, concentration has increased more than fourfold, driven by increases in cross-market concentration.

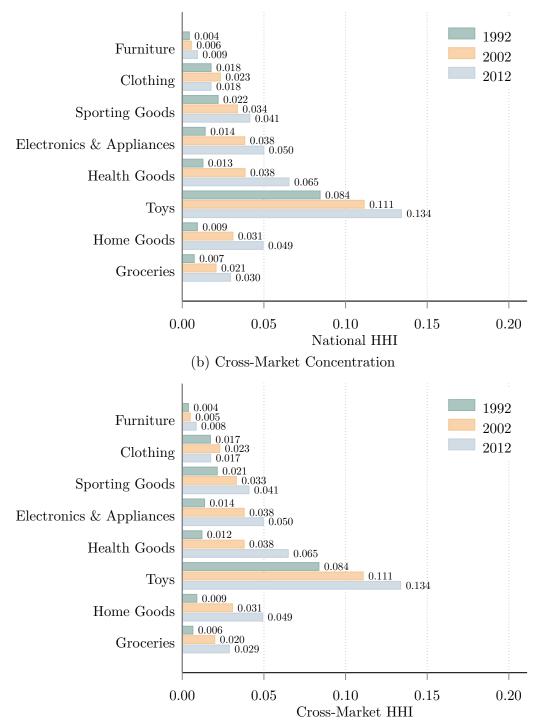


Figure 7: National and Cross-Market Concentration across Product Categories

(a) National Concentration

Notes: The numbers are national and cross-market Herfindahl-Hirschman Indexes (HHI) by product weighted by market size from the Census of Retail Trade microdata.

4.4 Impact of Online and Other Non-Store Retailers

The previous results calculated local concentration using only brick-and-mortar retailers. Online and other non-store retailers were not included because our data do not let us see in which markets these retailers sell their goods. In what follows we consider the potential impact of non-store retailers on local concentration.

The market share of non-store retailers has more than tripled between 1992 and 2012. However, the overall importance of non-store retailers remained limited through 2012. The initial sales share of non-store retailers is low, just 2.7 percent in 1992. This low share reflects the absence of online retailers and the limited role of other retailers that rely on mail order and telephone sales. By 2012, the sales share of non-store retailers had risen to 9.5 percent, driven by an increase in online sales. By 2012, non-store retailers had significant market share in certain products, such as Furniture, Clothing, and Sporting Goods, but almost no market share in Groceries and Home Goods (see Appendix D.3).

The effect of online and other non-store retailers on local concentration depends on how their sales are distributed across and within markets. Unfortunately, the CRT does not record the location in which non-store retailers sell their products, making it impossible to determine the exact effect of these retailers on local concentration. Nevertheless, we can generate bounds for the effect of non-store retailers while being consistent with their behavior at the national level. To do this, we assume that the share of retail spending that goes to non-store retailers is constant across markets within a product category and is equal to the national sales share of non-store retailers in that category.

Having distributed the sales of non-store retailers across markets, we can construct an upper and a lower bound for the local HHI. Accounting for the sales of non-store retailers mechanically reduces the sales share of brick-and-mortar stores, which by itself reduces concentration, but the total effect on concentration depends on how concentrated nonstore retailers are. We construct an upper bound for this effect by assigning all the sales of non-store retailers to a single stand-in firm. Calculating concentration in this way is an upper bound under the assumption that firms do not have both brick-and-mortar and non-store establishments, which is consistent with the data. The lower bound assumes that non-store retailers are atomistic, with the sales share of each individual non-store retailer equal to zero. The two bounds are

$$HHI = (1 - s_{NS})^2 HHI_{BM}$$
 and $\overline{HHI} = (1 - s_{HS})^2 HHI_{BM} + s_{NS}^2$

where s_{NS} corresponds to the sales share of non-store retailers and HHI_{BM} to the HHI already computed for brick-and-mortar stores.

Figure 8 shows the bounds we construct for local concentration across product categories in the retail sector. As expected, including non-store retailers for categories like Home Goods or Groceries hardly affects the level of concentration since the market share of nonstore retailers remains low throughout. The effects are larger for the other categories, especially for 2012. Interestingly, the diluting effect of accounting for non-store retailers dominates in most categories, with the bounds for local concentration lying below the estimated HHI for brick-and-mortar stores (marked by the diamonds in the figure). It is only in Electronics and Appliances, and to a lesser extent in Clothing, that the market share of non-store retailers is large enough for their inclusion to potentially increase concentration.

When non-store retailers are included, there is still a clear increase in local concentration between 1992 and 2002, although the levels are slightly lower. Moving from 2002 to 2012, the story becomes ambiguous, especially for product categories with a significant share of their sales going to non-store retailers. In many cases the bounds for 2012 contain the bounds for 2002, indicating that local concentration could either be increasing or decreasing depending on the concentration among non-store sales. At a national level, non-store retailers were not highly concentrated during this time period (Hortaçsu and Syverson, 2015). Thus, the increasing importance of non-store retailers is potentially decreasing local market concentration between 2002 and 2012.

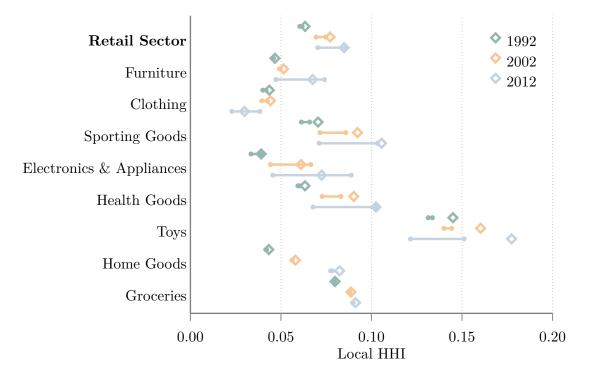


Figure 8: Local Concentration and Non-Store Retailers

Notes: The numbers are based on calculations from the Census of Retail Trade. Diamonds mark local concentration for brick-and-mortar stores as measured by the Herfindahl-Hirschman Index (HHI) at the commuting zone level. The continuous lines cover the bounds on concentration including non-store retailers. We assume that sales of non-store retailers are distributed across local markets proportionately to the sales of brick-and-mortar retailers. The upper bound assigns all the sales of non-store retailers to a single stand-in firm. The lower bound assumes that non-store retailers are atomistic, with the sales share of each individual non-store retailer equal to zero.

5 Markups and Local Concentration

In the previous sections, we showed that local concentration increased by 2.1 percentage points, on average, between 1992 and 2012. These changes can imply higher markups and ultimately affect consumer prices. However, studying this relationship is challenging because long series on prices and costs for U.S. retailers are not available. Nevertheless, linking changes in concentration to changes in prices is critical to assess the potential impact of concentration on consumers. To deal with data limitations, we use a standard model of Cournot competition based on the work of Atkeson and Burstein (2008) and Grassi (2017). This model provides us with an explicit link between the local HHI and average product markups. We find that increases in local concentration imply a 2.1 percentage point increase in markups between 1992 and 2012, roughly a third of the observed increase in markups during that period.

The model features strong parametric assumptions on firms to maintain tractability. In particular, we assume that 1) firms face isoelastic demand curves, with elasticities of demand varying by product but not by location, 2) firms operate a constant returns to scale technology, and 3) pricing decisions are taken at the market level, ignoring links between stores of the same firm across locations. Under these assumptions, the competitive environment faced by a firm is completely described by the firm's local market share. This allows us to link local concentration, as measured by the local HHI, to prices and markups without firm-level data on prices or costs. In this way, our model is limited by the extent to which the distribution of market shares captures the competitive environment in retail markets. In Appendices F.4.1 and F.4.3 we discuss how to relax some of the assumptions listed above and the effects on our results.

The model economy contains I firms operating in L different locations (representing commuting zones) where J different products are traded. Firms compete in quantities in a non-cooperative fashion and have market power in the local product markets in which they operate.¹⁹ A market is characterized by a pair (j, ℓ) of a product and a location, with an isoelastic demand curve for each product. Firms produce using only labor and differ only in their productivity, $z_i^{j\ell}$. We assume labor to be immobile across locations, so each location has a specific wage, w_{ℓ} . Thus, the firm's marginal cost is $\lambda_i^{j\ell} \equiv w_{\ell}/z_i^{j\ell}$. A complete description of the model is in Appendix F.

The solution to each firm's problem is to charge a market-specific markup, $\mu_i^{j\ell}$, over 19 In Appendix F.1.2 we solve the model for competition in prices and monopolistic competition.

the firm's marginal cost so that the price is $p_i^{j\ell} = \mu_i^{j\ell} \lambda_i^{j\ell} \lambda_i^{j\ell}$.²⁰ The markup is characterized in terms of the firm's market share, $s_i^{j\ell}$, and the product's elasticity of demand, ϵ_j :

$$\mu_i^{j\ell} = \frac{\epsilon_j}{(\epsilon_j - 1)(1 - s_i^{j\ell})}.$$
(5)

Markups will be larger for firms with higher market shares and for products with a less elastic demand. Importantly, equation (5) allows us to estimate markups using only data on market shares and elasticities of demand.

The model provides an explicit link between local retail concentration and markups faced by consumers. We use the firm-specific markups in equation (5) to derive closedform expressions for markups in each market (μ_j^{ℓ}) as well as for the average markup of each product nationally (μ_j) . Appendix F.2 presents the derivations. Both markups directly depend on the local HHI:

$$\mu_j^\ell = \frac{\epsilon_j}{\epsilon_j - 1} \left[1 - H H I_j^\ell \right]^{-1},\tag{6}$$

$$\mu_j = \frac{\epsilon_j}{\epsilon_j - 1} \left[1 - \sum_{\ell=1}^L s_\ell^j H H I_j^\ell \right]^{-1},\tag{7}$$

where HHI_j^{ℓ} is the HHI of product j in location ℓ and s_{ℓ}^j is the share of location ℓ in the national sales of product j. As the local HHI approaches zero, markups approach the Dixit-Stiglitz markups under monopolistic competition. As markets become more concentrated, average markups increase. The sensitivity of markups to increases in concentration is larger for products with a lower elasticity of demand.

²⁰Recent work has indicated that firms charge similar and even the same prices across locations in building material (Adams and Williams, 2019) and groceries (Dellavigna and Gentzkow, 2019). Whether the phenomenon holds more broadly is a subject for further research. Appendix F.4.3 shows that uniform pricing depends on a weighted average of local market power. Thus, our assumption of pricing-to-market should have a small effect on aggregate conclusions but may have distributional impacts.

5.1 Estimation and Data

The two key ingredients for analyzing markups are firms' market shares by product in each location, $s_i^{j\ell}$, and the elasticity of substitution for each product, ϵ_j . We obtain the shares directly from the CRT and estimate the elasticities using equation (7). Specifically, we use the product HHIs calculated in Section 4.2 and gross margins by industry from the Annual Retail Trade Survey (ARTS).

The ARTS provides the best, but not ideal, source to compare our results to because it computes markups using cost of goods sold and reports them for detailed industries. Markups using cost of goods sold are the most direct data analogue to markups in the model, as shown in Appendix F.2 and F.4.1. However, there are still issues with comparing the industry-level results in the ARTS to our product-level results. Industry markups and product markups may move in opposite directions due to changes in composition. For example, if low margin clothing stores have been replaced by lower margin general merchandise stores, markups in the clothing industry would rise, while markups on clothing would decrease. Nonetheless, the ARTS allows us to construct markup measures that are informative about product markups by focusing on the industries that specialize in each product category.

5.2 Changes in Concentration and Markups

We conduct two exercises with the model. First, we fit the model to match product markups in 1992 given the observed levels of local concentration. Doing this provides us with estimates of the elasticities of substitution. Holding these estimates fixed, we can extend the model through 2012 and obtain the change in markups implied by the observed increase in local concentration. Second, we can fit the model to match observed markups for each Economic Census year by allowing the elasticities of substitution to be time varying. These exercises give us a measure of the relative role of local concentration in explaining the observed changes in markups.

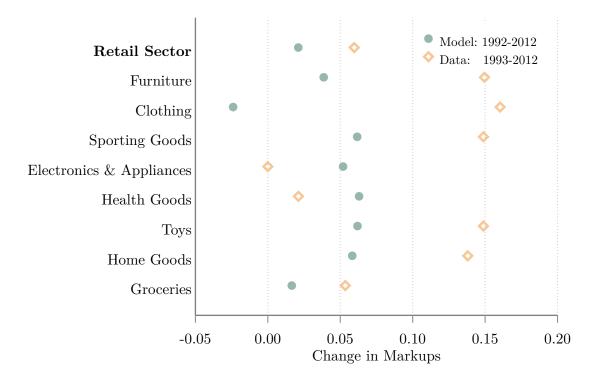


Figure 9: Local Concentration and Markups

Notes: Diamonds mark the change in markups between 1992 and 2012 from the Annual Retail Trade Survey data for the main industry for each product category and a weighted average across products. Circles mark the change in markups implied by the change in local concentration given the model estimates for 1992.

The increase in local concentration implies an increase in retail markups of 2.1 percentage points between 1992 and 2012, but this falls short of the 6 percentage point increase in markups implied by the ARTS. Figure 9 shows that in all but two product categories, the observed increase in markups in the main industry for the product is higher than what is implied by the rise in product-level HHI. The changes in model markups in Figure 9 assume that the elasticity of demand faced by firms are constant over time and vary only because of changes in local HHI. However, many changes in the competitive environment of retail can be reflected in changes in these elasticities rather than changes in market concentration.

Table 3 shows the value of the elasticity of substitution needed to match the level of markups in each year. We find the lowest elasticities of substitution in Clothing and

Product Category	1992	$\frac{\epsilon_j}{2002}$	2012
Furniture	2.54	2.32	2.33
Clothing	2.61	2.43	2.25
Sporting Goods	3.17	3.16	2.85
Electronics & Appliances	3.59	4.37	3.96
Health Goods	3.84	4.32	4.18
Toys	3.90	3.82	3.40
Home Goods	4.24	3.78	3.62
Groceries	5.44	4.57	4.87

Table 3: Estimated Elasticities of Substitution

Notes: The data are authors' estimates of product elasticities of substitution using industry markups from the Annual Retail Trade Survey and product-level local Herfindahl-Hirschman Indexes calculated from the Census of Retail Trade. The elasticities are the solution to equation (7).

Furniture. These are categories that feature many different brands only available from a small set of retail firms, leaving more room for differentiation than in products such as Toys and Groceries where different firms carry similar or even identical physical products.

To match the observed increase in markups, most product categories require a decrease in their elasticity of substitution. Of course the magnitude of the decrease depends on the initial level of the elasticities as markups respond more to changes for lower elasticities. For example, both Toys and Sorting Goods had an increase in markups of 8.7 percentage points that was not explained by the change in local concentration. For Toys, a decrease in elasticity of 0.5 was needed to explain this residual, while it was only 0.3 for Sporting Goods. The decreasing trend for the elasticities of substitution is consistent with the findings of Bornstein (2018), Brand (2020), and Neiman and Vavra (2020), who link the decrease to the rise of store and brand loyalty/inertia.

The exception to the trend of decreasing elasticities of substitution are Electronics and Appliances and Home Goods, which instead require an increase in their elasticities. Electronics and Appliances had no change in markups in the data, but based on the change in concentration, markups should have increased slightly over 5 percentage points. This product category is a good example of the limitations of using the ARTS. The main subsector for Electronics and Appliances, 443, accounts for only 31 percent of sales of this product category (Table D.1), leaving significant opportunity for divergence between product markups and industry markups.

Altogether, our results suggest that changes local concentration explain about one-third of the increase in markups, raising them from 1.44 in 1992 to 1.46 in 2012. These increases are small relative to the 34 percent decrease in the relative price of retail goods during this time period. The increases in markups and concentration may be the result of low-cost firms gaining market share, in which case the decrease in prices cannot be separated from the increase in concentration. Even if the implicit reduction in costs is realized without an increase in concentration, the decrease in prices would have been 35 percent.

6 Conclusion

Despite the attention given to the rise of national concentration in the U.S., less is known about the dynamics of local concentration and the relationship between observed national trends and the behavior of local markets. This paper helps to shed light on these issues by contributing in three related fronts. First, we decompose national concentration measures into a local component (national concentration rises as local markets become more concentrated), and a cross-market component (national concentration rises as the same firms are present in more markets, increasing their national market share). Second, we measure concentration at a granular level by compiling new Census microdata covering all U.S. retailers. Third, we estimate a model of oligopolistic competition that features an explicit link between the local HHI and markups to quantify the effect of concentration on retail markups.

We show that local concentration has almost no effect on national concentration

measures. Instead, cross-market concentration explains most of the increase in national concentration observed since 1992. That is, national concentration is driven by consumers in different locations shopping at the same firms, highlighting the role of large multi-market retailers in explaining the dynamics of the retail sector.

Our measures of local concentration show broad increases across locations and products since the 1990s, although they are at lower rates than the increases in national concentration. We link these changes to markups and find that they explain roughly a third of the increase in markups observed in the retail industries associated to our main product categories. We conclude from our findings that despite the stark increases in national concentration (doubling between 1997 and 2007), and broad-based changes in retail markets, increasing local concentration has had a limited effect on consumer welfare.

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Appendices

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A Comparison to Rossi-Hansberg, Sarte, and Trachter (2020)

This section compares our results to those in Rossi-Hansberg, Sarte, and Trachter (2020) (hereafter RST) for the retail sector and explains the factors contributing to the differences between our papers. Unlike us, they find a reduction in the local HHI for the retail sector between 1990 and 2014.²¹

There are three key differences between our paper and RST's that each partially explains the opposite results regarding local concentration. First, we use different data sources: while RST use the National Establishment Time Series (NETS), this paper uses confidential data from the CRT and the LBD. Second, we have different definitions of markets: this paper defines markets by product based on NAICS-6 classification of establishments, while RST define markets by industry based on SIC-8 or SIC-4 classification of establishments. Third, we differ in the methodology used to aggregate markets. This paper aggregates market-level concentration using contemporaneous weights, and we report the change in this (aggregate) index of local concentration. In contrast, RST aggregate the change in market-level concentration using end-of-period weights and report this (aggregate) change.

We argue that the CRT is likely to provide better data for the study of concentration in local markets, and we show that changing from NETS to CRT data alone explains a third of the discrepancy in the change of local concentration (while controlling for market definition and aggregation methodology). Another third of the difference in estimates is explained by the definition of product markets (by changing detailed SIC-8 industries to more aggregated SIC-4 industries). The proper definition of a product market (SIC-8, SIC-4, NAICS-6, product category) can depend on the question being asked. We argue in Section 3.3 that product categories are the proper way to study retail markets. The final third of the difference in estimates is explained by the aggregation methodology. We argue

²¹RST present results for many sectors of the economy. In what follows we discuss only their results in the retail sector. However, our discussion of aggregation methods is relevant for all sectors.

that the method used by RST is biased toward finding decreasing local concentration, and we show that their method could find evidence of decreasing concentration in a time series, even when concentration is not changing in the cross-section. This occurs when markets become less concentrated as they grow. Below we expand upon these differences and their implications for the measurement of local concentration.

Data sources The baseline results in RST are based on the NETS, a data product from Walls and Associates that contains information on industry, employment, and sales by establishments. These data have been shown to match county-level employment counts relatively closely (Barnatchez, Crane, and Decker, 2017), but the data do not match the dynamics of businesses Crane and Decker (2020). The results in this paper are based on the CRT, a data set assembled and maintained by the U.S. Census Bureau covering the universe of retail establishments.

Both the NETS data and the CRT use the establishment's reported industry and sales when available and both have some degree of imputation for establishments that do not report. However, the CRT can often impute using administrative records from the IRS.²² Beyond this, the two data sets differ in other two relevant aspects. First, the CRT contains sales by product category for the majority of sales, while the NETS contains only industry, allowing us to define markets by product categories and account for cross-industry competition by general merchandisers (see Section 3.3). Second, the NETS includes non-employer establishments, while the CRT does not. According to official estimates, non-employer establishments account for about 2 percent of retail sales in 2012 (Economy-Wide Key Statistics: 2012 Economic Census of the United States).²³ On the whole, the CRT provides a more accurate picture of activity in the retail sector.

²²Response to the CRT is required by law. Single-unit establishments are randomly sampled for sales in the CRT, while the non-sampled units have their sales imputed. See http://dominic-smith.com/data/CRT/crt_sample.html for more details.

²³https://factfinder.census.gov/faces/tableservices/jsf/pages/productview.xhtml?pid= ECN_2012_US_00A1&prodType=table

Definition of product markets We adopt a different definition than RST for what constitutes a product market. Each definition of product market has its own pros and cons, and researchers may choose one over the other depending on the specific context. We define markets by a combination of a geographical location and a product category that we construct using the detailed data on sales provided by the CRT, along with the (NAICS-6) industry classification of establishments (see Section 3.3). As we mentioned above, doing this treats multi-product retailers as separate firms, ignoring economies of scope, in favor of putting all sales in a product category in the same market.

In contrast, RST define markets by the establishment's industry, using both SIC-8 and SIC-4 codes. Some examples of SIC-8 codes are department stores, discount (53119901); eggs and poultry (54999902); and Thai restaurants (58120115).²⁴ SIC-8 codes may be overly detailed for retail product markets, to the point that many retailers will sell multiple types of goods. For example, calculating concentration in eggs and poultry (54999902) would miss the fact that many eggs and poultry are sold by chain grocery stores (54119904) and discount department stores (53119901). This suggests that aggregating to less detailed codes may provide a better definition of product markets. To that end, RST present results for SIC-4 codes. When concentration is calculated using SIC-4 codes, the decrease in local concentration is much smaller, a 8 percentage point decrease instead of a 17 percentage point decrease.²⁵

Incidentally, the SIC-4 codes are quite similar to the NAICS-6 codes available in the CRT, except restaurants are included in the SIC definition of retail but not in NAICS.²⁶ This makes the concentration measures based on each classification more closely comparable.

²⁴NETS allows for 914 retail SIC-8 codes. A full list is available at https://www.dnb.com/content/dam/ english/dnb-solutions/sales-and-marketing/sic_8_digit_codes.xls. RST indicate that many SIC-8 codes are rarely used (data appendix), but without access to the NETS data, we cannot assess the relative significance of each code for economic activity.

²⁵The change from SIC-8 to SIC-4 has little effect on concentration outside of retail (RST Data Appendix). The numbers are read off graphs for the change in retail sector concentration for zip codes between 1990 and 2012.

 $^{^{26}}$ In the results in the main text, we exclude automotive dealers, gas stations, and non-store retailers because of concerns related to ownership data and defining which markets they serve (see Section 3 for further discussion). This has little impact on the estimates for local concentration.

Yet, even in this setting (NETS SIC-4 versus CRT NAICS-6) there are still significant differences between our studies. We will go back to this comparison when we discuss Figure A.2 and Table A.1 below.

Aggregation methodology The final difference comes from how we aggregate the market-level changes in concentration into an aggregate index of local concentration. We compute the local HHI index by first computing the HHI for each pair of product category (j) and location (ℓ) . Then we aggregate across locations, weighting each market (location-product) HHI by the market's share of the product's national sales. Doing this provides a measure of the average local HHI for each product. Finally, we aggregate across products, weighting by the product's share of national retail sales, to obtain an average local HHI. We do this for each period (t) and report the time series for this index. The average local HHI is then given by

$$HHI_{t} = \sum_{\substack{j \\ Products}} s_{j}^{t} \sum_{\substack{\ell \\ Locations}} s_{\ell}^{jt} \cdot HHI_{j\ell t}, \quad \text{where } HHI_{j\ell t} = \sum_{i} \left(s_{i}^{j\ell t}\right)^{2}.$$
(A.1)

RST use a different methodology. Instead of computing concentration in the crosssection, they calculate the change in concentration between t and some initial period and then aggregate these changes weighting by the period t share of employment of each industry (j) in total retail employment. Their index for the change in concentration is given by²⁷

$$\Delta HHI_t^{RST} = \sum_{j\ell} s_{j\ell}^t \Delta HHI_{j\ell t}, \qquad (A.2)$$

where $s_{j\ell}^t$ is the sales share of industry j and location ℓ in the country at time t^{28} and $\Delta HHI_{j\ell t}$ is the change in the revenue-based HHI in industry j and location ℓ between the

 $^{^{27}}$ Equation A.2 is taken from RST, with notation adjusted to match the notation in this paper.

²⁸Note that RST weight markets by their employment share $\begin{pmatrix} e_{j\ell}^t \end{pmatrix}$ instead of their sales share $\begin{pmatrix} s_i^{j\ell t} \end{pmatrix}$. However, their data appendix shows this has no effect on the results.

base period and time t.

The key difference between the methodologies is that RST do not account for the size of a market in the initial period. This is shown in equation A.3, which subtracts the two measures of concentration from each other. After canceling terms, the difference between the two measures is

$$\Delta HHI - \Delta HHI^{RST} = \sum_{j\ell} \underbrace{(s_{j\ell}^t - s_{j\ell}^0)}_{\Delta s_{j\ell}^t} \cdot HHI_{m\ell 0}.$$
(A.3)

RST will weight markets that increase in size over time by more in the initial period, while those that decrease will be weighted less relative to our measure. As markets grow, they typically become less concentrated resulting in RST weighting markets with decreasing concentration more than markets with increasing concentration.²⁹

Figure A.1 shows that this methodology can find decreasing concentration in a time series, even when concentration is not changing in the cross-section. Consider three firms (A, B, and C) that operate in two markets and have the same size. In the first period (t-1), firms A and B operate in market 1 and firm C operates in market 2. Consequently, the HHI is 0.5 and 1 for each market, respectively, and the aggregate (cross-sectional) HHI is 2/3. In period t, market 1 shrinks and market 2 grows, with firm B changing markets. This change does not affect the cross-sectional distribution of local (market-specific) concentration, but it does imply an increase in concentration in market 1 and a decrease in market 2. Despite there being no changes in the cross-sectional HHI, RST's methodology would report a decrease in local concentration ($\Delta HHI = -1/6$), driven by the decrease in market 2's HHI (which happens to be the largest market in period t).

 $^{^{29}\}mathrm{A}$ similar point is made in Appendix E of Ganapati (2020) using LBD data.

Quantifying differences Figure A.2 quantifies the role of each of the differences highlighted above for the change in local concentration between 1992 and 2012.³⁰ To make the comparison clear, we define markets by industry throughout the exercise.³¹ Overall, Figure A.2 shows that the difference in the estimated change of local HHI is explained in roughly equal parts by the three differences highlighted above: data source (CRT versus NETS), industry definition (NAICS-6 versus SIC-8), and aggregation methodology. We discuss each step in more detail below.

The lowest estimate for the change in local concentration (a decrease of 0.17 points in local HHI) corresponds to RST's baseline estimate using NETS data and SIC-8 for industry classification. Once industries are aggregated to the SIC-4 level (to improve comparability across establishments), the estimate increases by 9 percentage points, still implying a reduction of 8 percentage points in the local HHI. The next estimate reproduces RST's methodology using microdata from the CRT. Changing from NETS to CRT data implies a further increase in the estimate of 6.5 percentage points, with the overall change suggesting a minor decease of local HHI of 1.5 percentage points.³² Next we change the weighting methodology to ours (as explained above). Doing so increases the estimated change of local concentration again (by 9.5 percentage points), implying an overall increase of local HHI of 8 percentage points.

Table A.1 provides a more detailed account of the estimates presented in Figure A.2 and also includes estimates of changes in local concentration for intermediate census years (1997, 2002, and 2007). In the first panel, national concentration, we compare the numbers in RST (Figure 1b) to numbers calculated for NAICS-based measures (including all 6-digit industries in NAICS) and product-based measures. In all three cases, national

 $^{^{30}\}mathrm{RST}$ use 1990 as the base year instead of 1992. This is unlikely to matter as RST find small changes in concentration between 1990 and 1992.

³¹To be precise, we define a market either by an SIC-8, an SIC-4, or a NAICS-6 industry in a given location. Our preferred definition of markets by product categories implies a change in the level of the HHI that makes the comparison with the results in RST less transparent.

³²Part of this difference could be explained in theory by the inclusion of restaurants in SIC-4; however, the industry by industry results in RST's Figure 7 suggest that this is not the case because they find diverging trends in most retail industries.

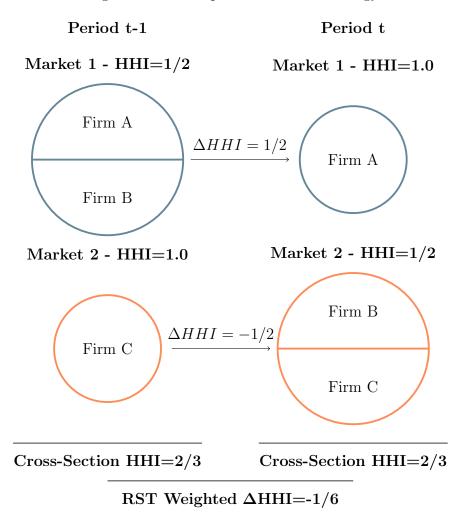
concentration is increasing significantly. Despite differences in the initial levels of concentration (column 1), the national HHI increases by two to three times.³³

The second panel of Table A.1 compares concentration measured at the zip code level using RST's weighting methodology as described above. We also provide results for the set of establishments that are included in the product-based results in the paper. Using their methodology, we find evidence for slight decreases in local concentration of 1 to 2 percentage points whether markets are aggregated using sales or employment weights. These decreases are much less severe than the 17 percentage point decrease in RST.

The final panel of Table A.1 compares concentration measured at the zip code level using our aggregation method. This method finds significant increases in local concentration across both NAICS samples. Local HHI increased between 7.1 and 8.5 percentage points; that is, the average dollar in 2012 is spent in a more concentrated market than the average dollar in 1992.

 $^{^{33}\}mathrm{The}$ level of concentration is not provided in RST.

Figure A.1: Example of RST Methodology



Notes: The figure shows how market and cross-sectional concentration indices are computed under our methodology (difference in cross-section Herfindahl-Hirschman Index (HHI)) and that of Rossi-Hansberg et al. (2020). The economy has two markets and three firms. Firms are of the same size. Markets change size from period t - 1 to period t, but the cross-sectional distribution of markets and concentration does not change. The weighting methodology used by Rossi-Hansberg et al. (2020) puts more weight on market 2, which increases size between t - 1 and t and has a reduction in concentration. The result is a decrease in aggregate concentration when changes are measured according to this methodology, while cross-section HHI does not change.

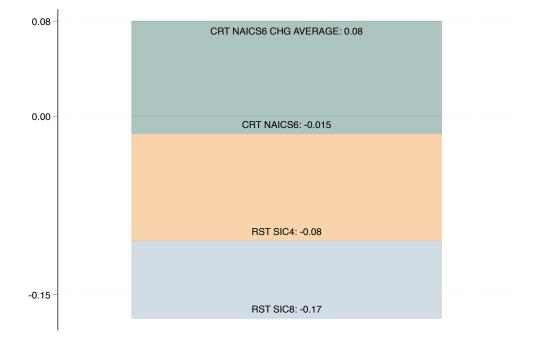


Figure A.2: RST Comparison

Notes: The figure shows various estimates for the change in local HHI between 1992 and 2012. The estimates vary according to the data source, industry definition, and aggregation methodology. The lowest estimate corresponds to Rossi-Hansberg et al. (2020)'s estimate using SIC-8 industries, and the second lowest estimate corresponds to using SIC-4 industries. The second highest estimate corresponds to using Census of Retail Trade microdata and NAICS-6 industries (which are similar to SIC-4 industries), and the highest estimate computes indices under our aggregation methodology instead of that of Rossi-Hansberg et al. (2020).

National Concentration								
	TT7 · 1 /	Level	Change from 1992					
	Weight	1992	1997	2002	2007	2012		
RST	Emp.	N/A	0.020	0.030	0.050	0.055		
NAICS Based	Sales	0.029	0.017	0.056	0.076	0.087		
Product Based	Sales	0.013	0.006	0.018	0.029	0.030		
Zip Code Concentration: End-of-Period Weights								
	Weight	Level		Change from 1992				
RST	Emp.		-0.070	-0.100	-0.140	-0.170		
NAICS Based	Emp.		-0.022	-0.016	-0.019	-0.015		
NAICS Dased	Sales	N/A	-0.023	-0.015	-0.017	-0.011		
Dan en Camarla	Emp.		-0.002	-0.013	-0.018	-0.017		
Paper Sample	Sales		-0.024	-0.009	-0.013	-0.011		
Product based	N/A		N/A	N/A	N/A	N/A		
Zip Code Concentration: Current Period Weights								
	Weight	Level		Change from 1992				
RST	N/A	N/A	N/A	N/A	N/A	N/A		
NAICS Based	Emp.	0.507	0.025	0.060	0.068	0.080		
MAIUS Dased	Sales	0.498	0.018	0.052	0.062	0.071		
Danan Cample	Emp.	0.524	0.029	0.069	0.075	0.083		
Paper Sample	Sales	0.530	0.022	0.073	0.081	0.085		
Product Based	Sales	0.2637	0.013	0.024	0.022	0.013		

Table A.1: Comparison of Concentration to RST

Notes: The numbers come from the Census of Retail Trade and Rossi-Hansberg et al. (2020) (RST). Numbers from RST are taken from retail series in Figure 2. The level column contains the 1992 level of concentration. The formula for changes in concentration using end-of-period weights does not depend on the initial 1992 level as shown in RST, and consequently the level column does not apply to these calculations. NAICS-based measures concentration calculated including all NAICS industries. Paper sample uses only establishments included in the sample for the product-based results. Retail in RST is defined using SIC codes that include restaurants.

B Concentration Decomposition

The Herfindahl-Hirschman Index for the retail sector is given by the sales-weighted average of the product-HHI:

$$HHI^t \equiv \sum_{j=1}^J s_j^t HHI_j^t.$$
(B.1)

The HHI for a given product can be decomposed into the contribution of local and cross-market concentration. This section provides additional details on the concentration decomposition. The decomposition starts from the probability that two dollars (x, y) are spent at the same firm (i), which gives the HHI at the national level:

$$HHI_{j}^{t} \equiv P(i_{x} = i_{y}; j, t) = \sum_{\ell=1}^{L} \sum_{i} \left(s_{i}^{j\ell t}\right)^{2}.$$
 (B.2)

This probability can be divided into two terms:

$$P(i_{x} = i_{y}; j, t) = \underbrace{P(i_{x} = i_{y} | \ell_{x} = \ell_{y}; j, t)}_{\text{Local Term}} \underbrace{P(\ell_{x} = \ell_{y}; j, t)}_{\text{Collocation}} \underbrace{P(\ell_{x} = \ell_{y}; j, t)}_{\text{P}(\ell_{x} = \ell_{y}; j, t)} \underbrace{P(\ell_{x} = \ell_{y}; j, t)}_{P(\ell_{x} \neq \ell_{y}; j, t)} \underbrace{P(\ell_{x} \neq \ell_{y}; j, t)}_{P(\ell_{x} \neq \ell_{y}; j, t)}$$
(B.3)

Cross-Market Term

When we report contribution of local and cross-market concentration for the retail sector, we report the sales-weighted average of these two terms across products.

The collocation probability is calculated as:

$$P(\ell_x = \ell_y; j, t) = \sum_{\ell}^{L} \left(s_{\ell}^{jt}\right)^2.$$
(B.4)

When we report the collocation for the retail sector, we report the sales-weighted average of collocation across products: $\text{Collocation}_t = \sum_j s_j^t P(\ell_x = \ell_y; j, t).$

Local concentration is calculated as:

$$P(i_{x} = i_{y}|\ell_{x} = \ell_{y}; j, t) = \sum_{\ell=1}^{L} \underbrace{P(\ell_{x} = \ell|\ell_{x} = \ell_{y}; j, t)}_{\text{Location Weights}} \underbrace{P(i_{x} = i_{y}|\ell_{x} = \ell, \ell_{x} = \ell_{y}; j, t)}_{\text{Equation Weights}}$$
$$= \sum_{\ell=1}^{L} \frac{(s_{\ell}^{jt})^{2}}{\sum_{n} (s_{n}^{jt})^{2}} \sum_{k=1}^{K} \left(s_{k}^{j\ell t}\right)^{2}$$
(B.5)

This probability can be further decomposed into a term due to the average number of firms in each market (location) and a term due to the inequality of shares across firms within a market:

$$\begin{split} P\left(i_x = i_y | \ell_x = \ell_y; j, t\right) &= \sum_{\ell=1}^L s_\ell^{jt} \left(\frac{1}{N_\ell} + \sum_{k \in K_\ell} \left(s_k^{j\ell t} - \frac{1}{N_\ell} \right)^2 \right) \\ &= \sum_{\ell=1}^L s_\ell^{jt} \frac{1}{N_\ell} + \sum_{\ell=1}^M s_\ell^{jt} \sum_{i \in K_\ell}^K \underbrace{\left(s_k^{j\ell t} - \frac{1}{N_\ell} \right)^2}_{\text{Inequality of shares}} \end{split}$$

When we report the local HHI for individual product categories we also report the retail sector's average local HHI using sales weights instead of the weights implied by the decomposition to facilitate comparison to other research such as Rinz (2020) and Lipsius (2018):

$$\operatorname{HHI}_{t}^{\operatorname{Local}} = \sum_{j}^{J} s_{j}^{t} \sum_{\ell}^{L} s_{\ell}^{jt} \sum_{i} \left(s_{i}^{j\ell t} \right)^{2}$$
(B.6)

The cross-market term is calculated as:

$$P\left(\ell_{x} = \ell_{y}; j, t\right) P\left(i_{x} = i_{y} | \ell_{x} \neq \ell_{y}; j, t\right) = \left(1 - \sum_{\ell=1}^{L} \left(s_{\ell}^{jt}\right)^{2}\right) \sum_{k=1}^{L} \sum_{\ell \neq k} \frac{s_{k}^{jt} s_{\ell}^{jt}}{1 - \sum_{m}^{L} \left(s_{m}^{jt}\right)^{2}} \sum_{i=1}^{I} s_{i}^{jkt} s_{i}^{\ell jt}$$
$$= \sum_{k=1}^{L} \sum_{\ell \neq k} s_{k}^{jt} s_{\ell}^{jt} \sum_{i=1}^{I} s_{i}^{jkt} s_{i}^{j\ell t}.$$

This calculation is the same in the results for product category because $1 - \sum_{m}^{L} (s_{m}^{jt})^{2}$ cancels in the calculation of the collocation term.

C Cleaning and Aggregating Product Lines Data

The Economic Census collects data on establishment-level sales in a number of product categories (Figure C.1 provides an example form). Many establishments have missing product line sales either due to them not responding to questions or because they do not receive a form.³⁴ In total, reported product lines data account for about 80 percent of sales. We develop an algorithm to impute data for missing establishments, which involves aggregating product line codes into categories such that we can accurately infer each establishment's sales by category with available information. For example, we aggregate lines for women's clothes, men's clothes, children's clothes, and footwear into a product category called clothing.

We then establish 18 product categories detailed in Table C.1. Of these 18 product categories, 8 categories that we label "Main" account for over 80 percent of store sales in the sample. The other 10 product categories are specialty categories that account for a small fraction of aggregate sales and are sold primarily by establishments in one specific industry. For example, glasses are sold almost exclusively by establishments in 446130 (optical goods stores). We create these categories so that establishments that sell these products are not included in concentration measures for the 8 main product categories.

C.1 Aggregating Product Lines

The first step of cleaning the data is to aggregate reported broad and detailed product line codes into categories. Some codes reported by retailers do not correspond to valid product line codes, and we allocate those sales to a miscellaneous category. The Census analyzes reported product line codes to check for issues and flags observations as usable if they pass this check. We include only observations that are usable and then map these codes to categories. We use the reported percentage of total sales accounted for by each product line instead of the dollar value because the dollar value is often missing. Typically

³⁴Establishments of large firms are always mailed a form, but small firms are sampled.

Figure C.1: Sample Product Lines Form

Item 10. MERCHANDISE LINES Report sales for each merchandise line sold by this establishment, either as a dollar figure or as a whole percent of total sales. (See HOW TO REPORT DOLLAR FIGURES on page 1 and HOW TO REPORT PERCENTS below)								
HOW TO REPORT	∕₀ of	Mil.	Thou.	Dol.	Per- cent			
PERCENTS • Report whole pe	Report whole percents-				39			
Not acceptable -			1	→	38.76			
Merchandise lines	Cen-	ESTIMATES are acceptable. Report dollars OR percents.						
merchandise miles	use	Mil.	Thou.	Dol.	Per- cent			
 Women's, juniors', and misses' wear (Report girls' and infants' and toddlers' wear on line 3 and footwear on line 4) 	230 0220	231			232			
 Men's wear (Report boys' wear on line 3 and footwear on line 4) 	0200							
 Children's wear (Include boys' (sizes 2 to 7 and 8 to 20), girls' (sizes 4 to 6x and 7 to 14), and infants' and toddlers' clothing and accessories. Report footwear on line 4.) 	0240							
4. Footwear (include accessories) FORM RT-5302	0260							

101101111-5502

an establishment either reports product line data for 100 percent of its sales or does not report any data. For the small number of establishments that report product lines data summing to a number other than 100 percent, we rescale the percentages so that they sum to one.³⁵ After this procedure, we have sales by product category for all establishments that reported lines data. The resulting categories are listed in Table C.1.

³⁵This procedure has a minimal effect on aggregate retail sales in each category.

Product Category	Main	Corresponding Industry	Example Firm		
Automotive Goods	Ν	441	Ford Dealer		
Clothing	Υ	448	Old Navy		
Electronics and Appliances	Υ	443	Best Buy		
Furniture	Υ	442	Ikea		
Services	Ν	N/A			
Other Retail Goods	Ν	N/A			
Groceries	Υ	445	Trader Joe's		
Health Products	Υ	446	CVS		
Fuel	Ν	447	Shell Gasoline		
Sporting Goods	Υ	451	Dick's Sporting Goods		
Toys	Υ	451	Toys "R" Us		
Home & Garden	Υ	444	Home Depot		
Paper Products	Ν	453210			
Jewelry	Ν	423940	Jared		
Luggage	Ν	448320	Samsonite		
Optical Goods	Ν	446130	Lenscrafters		
Non-Retail Goods	Ν	N/A			
Books	Ν	451211	Borders		

Table C.1: List of Product Categories

Notes: Authors' created list of product categories. The Main column indicates that a product category is included in concentration calculations. Firm names were created for illustrative purposes based on industries reported to the Securities and Exchange Commission and do not imply that the firm is in the analytical sample.

C.2 Imputing Missing Data

For the remaining establishments, we impute data using the NAICS code of the establishment, reported sales of other establishments of the same firm in the same industry, and reported activity of the same establishment in other census years.³⁶ Most establishments are part of single-unit firms, and many do not appear in multiple census years; thus their sales are imputed using only industry information.

Using this aggregation method, almost all establishments have significant sales in only two product categories, which increases confidence in the imputation. Additionally, we

 $^{^{36}}$ Reported product line sales are very similar across establishments of the same firm and the same establishment over time.

have compared the aggregate sales in our data to the Consumer Expenditure Survey (an independent Bureau of Labor Statistics program), and they are in line with the numbers from that source.³⁷

Where relevant, all sales are deflated using consumer price indexes. We use the food deflator for Groceries, clothing and apparel deflator for Clothing, and the deflator for all goods excluding food and fuel for all other categories.

We find that this procedure predicts sales accurately for most establishments, but a small number of stores in each industry report selling very different products than all other stores in that industry. In these cases, the prediction can produce substantial error.

³⁷Retail sales include some sales to companies, so it is expected that retail sales in a product category exceed consumer spending on that category.

D Additional Tables and Figures

D.1 The Role of Multi-Product Retailers

Table D.1 shows how sales for each main product category are distributed across sets of industries. This informs us of which type of establishment accounts for the sales of each product. The main subsector column refers to the NAICS subsector that most closely corresponds to the product category. The NAICS code of the subsector is indicated next to each product category. The main subsector accounts for just over half of sales on average, but this figure varies depending on the product. A larger fraction of sales of Furniture, Home Goods, and Groceries comes from establishments in their respective NAICS subsectors, while Electronics and Toys are more commonly sold by establishments in other subsectors. Over time, the share of sales accounted by the product's own subsector has decreased for most products, with the difference captured by establishments outside of the general merchandise subsector.

	Main Subsector			GM			Other		
	1992	2002	2012	1992	2002	2012	1992	2002	2012
Furniture (442)	76.3	73.1	64.4	16.9	13.3	11.2	6.8	13.6	24.4
Clothing (448)	50.9	51.8	51.1	41.4	37.7	27.4	7.7	10.5	21.5
Sporting Goods (451)	55.4	52.3	54.2	30.7	29.1	21.2	14.0	18.7	24.6
Electronic & Appliances (443)	30.3	31.0	29.5	34.1	27.1	24.9	35.6	41.9	45.6
Health Goods (446)	49.0	50.0	46.8	19.0	21.3	20.5	32.0	28.7	32.6
Toys (451)	40.7	27.6	22.0	45.2	47.7	46.9	14.1	24.7	31.1
Home Goods (444)	63.9	72.8	72.4	17.2	11.6	10.9	18.9	15.6	16.6
Groceries (445)	79.8	67.2	59.7	6.6	16.2	22.8	13.6	16.6	17.5
Average	55.8	53.2	50.0	26.4	25.5	23.2	17.8	21.3	26.8

Table D.1: Share of Product Category Sales by Establishment Subsector

Notes: The numbers come from the Census of Retail Trade data. GM includes stores in subsector 452. Other includes sales outside of the main subsector (indicated in parenthesis) and GM. Average is the arithmetic mean of the numbers in the column.

D.2 Extended Sample

We now present results with an extended sample that covers the period 1982 to 2012. The 1982 and 1987 Censuses of Retail Trade do not include product-level sales for all the categories we consider in our main sample (1992-2012). The affected product categories, Toys and Sporting Goods, account for a relatively small share of total retail sales. Therefore, we focus on results for the retail sector as a whole which we believe are reliable for this time period.

Figure D.1 presents measured concentration indexes for different definitions of local markets and the retail sector as a whole going back to 1982. Relative to Figure 3 we also include a measure of local concentration where markets are defined by Metropolitan

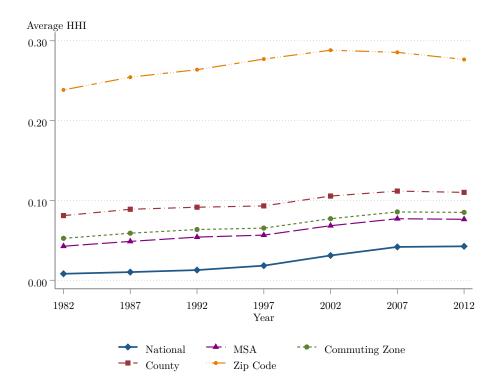


Figure D.1: National and Local Concentration

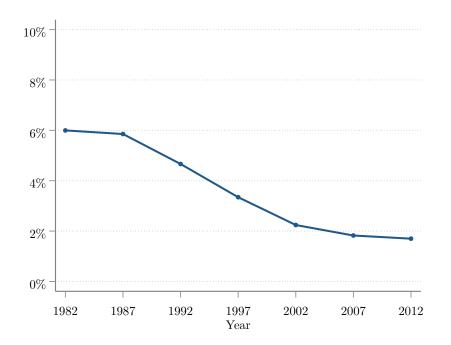
Notes: The data are from the Census of Retail Trade. The Herfindahl-Hirschman Index (HHI) for four different geographic definitions of local markets and national concentration are plotted. The local HHI is aggregated using each location's share of national sales within a product category. The numbers are sales weighted averages of the corresponding HHI in the product categories.

Statistical Areas (MSA). There are more MSAs than commuting zones (about 900 vs 722) and MSAs do not partition the U.S., omitting rural areas. In practice, the measured concentration level for MSAs is similar to that of commuting zones and only slightly lower.

Extending our sample to 1982 does not change the main result of increasing national and local concentration. All measures show sustained increases between 1982 and 2002. Looking at the full sample highlights the change in the rate of increase of national concentration after 1997 which contrasts with the slow increase during the 1980s.

Finally, we extend the decomposition exercise of Figure 4 to 1982. The results, shown in Figure D.2, show a stark decrease in the contribution of local concentration to national concentration. Even though the role of local concentration was never large (always below 6 percent), the share of national concentration attributed to local concentration fell sharply during the 1990s, ending at roughly 2 percent in 2002.

Figure D.2: Share of Local Concentration Term in National Concentration



Notes: The numbers are from the Census of Retail Trade. The share of local concentration is measured as the ratio of the local concentration term in equation (3) to the national Herfindahl-Hirschman Index (HHI). We aggregate the local concentration terms across the product categories using their sales shares.

D.3 Non-Store Retailer Market Shares

The penetration of non-store retailers varies widely across products. As Figure D.3 shows, the sales share of non-store retailers is highest in Electronics and Appliances, with an initial share of 7.5 percent in 1992 and a share of 20.9 percent in 2012. The initial differences were large, with only two categories (Electronics and Sporting Goods) having a share of more than 5 percent. By 2012, non-store retailers accounted for more than 15 percent of sales in five of the eight major categories. Despite this widespread increase, not all products are sold online. By 2012, only 0.7 percent of Groceries sales and 3 percent of Home Goods sales were accounted for by non-store retailers. These two categories account for almost half of all retail sales, which explains the overall low sales share of non-store retailers.

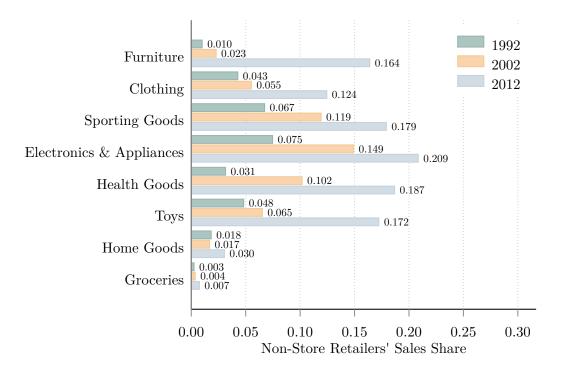


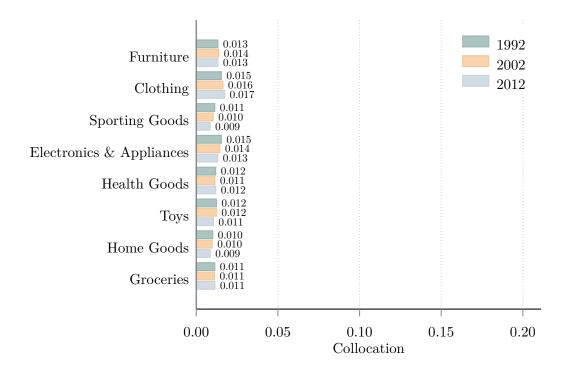
Figure D.3: Non-Store Retailers Share across Product Categories

Notes: The numbers are the national sales shares of non-store retailers by product category from the Census of Retail Trade microdata.

D.4 The Collocation Term and Local Concentration

Figure D.4 shows the collocation term by product category. The numbers are the probability that two random dollars are spent in the same commuting zone for each year. These numbers are small, less than 2 percent, and stable over time. There is also little variation across product categories because spending on product categories is approximately proportional to each market's size. These numbers form the weights for the local HHI in the decomposition of national concentration. Their small magnitude explains the limited role of local concentration in explaining national changes. The contribution of local concentration varies across products but it is always low. By the early 1990s, only furniture and groceries have contributions of over 10 percent, with the local contribution in all other products being no higher than 5.5 percent, and as low as 2 percent.





Notes: The data are from the CRT microdata. Numbers are the collocation term for commuting zones which forms the weight for the local HHI in the decomposition of national concentration.

E Industry-Based Results

A central contribution of this paper is the creation of store-level sales by product category for all U.S. retail stores. This allows us to define competition based on products rather than industry-based measures. Industries, either NAICS or standard industrial classification (SIC) codes, are regularly used to define markets. This approach is often necessitated by data availability and in many sectors is likely to be a good approximation (e.g. manufacturing).

This is not the case in the retail sector. The retail sector has one set of industries, general merchandise stores (NAICS 452), that compete with stores in many industries. By construction these industries are composed by establishment that sell many types of products. Thus, industry-based measures ignore the competition faced by stores selling a given product, coming from general merchandise stores. The measures we developed in Section 4 overcome this shortcoming.

Figure E.1 shows national and local concentration for the main subsector (3-digit NAICS) of each of our product categories. Local concentration is defined at the commuting zone level. The increasing trends we documented for national concentration in the retail sector are present in all subsectors, but the increase is particularly strong for general merchandisers (NAICS 452) both at the national and at the local level. Industry based measures of concentration miss the impact of increasing concentration among general merchandisers across product markets. Similar patterns arise in local concentration. Figure E.1b shows local concentration for the major subsectors, calculated as a weighted average of the industries comprising each subsector. Local industry concentration also increases.

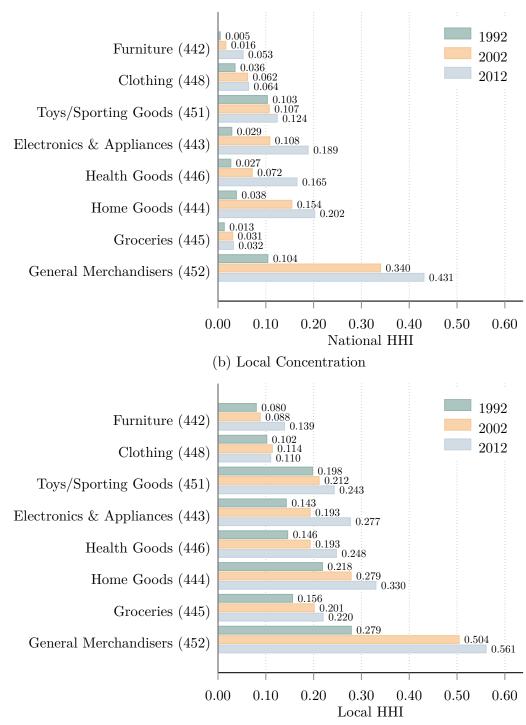
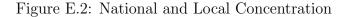
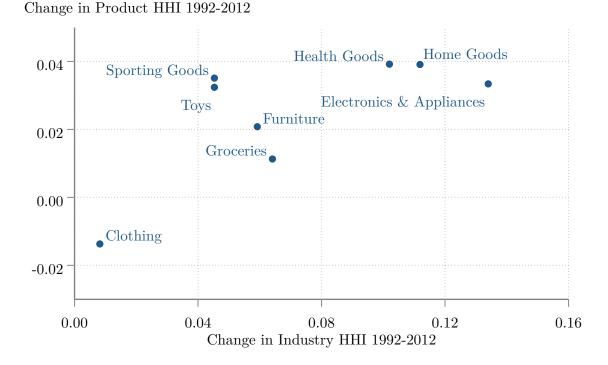


Figure E.1: National and Local Concentration Across Industries

(a) National Concentration

Notes: The data are from the Census of Retail Trade. Numbers are the national and Herfindahl-Hirschman Index (HHI) for various industries weighted by market size.





Notes: The data are from the Census of Retail Trade. Each point marks the change in local Herfindahl-Hirschman Index (HHI) of a product category and its main subsector between 1992 and 2012. Markets are defined at the commuting zone level.

Figure E.2 shows changes in product and industry based measures of local concentration. Despite changes in the level of the HHI both measures imply increasing concentration across most products/industries. Figure E.2 also makes clear that empirically there appears to be a correlation between product and industrial concentration, but this correlation is not perfect. Moreover, the significant sales share of non-store and general merchandise firms in most product categories means that this positive correlation could go away at any time.

F Model of Firm's Markups

We now provide more detail on the model described in section 5. We follow Grassi (2017) who builds on Atkeson and Burstein (2008). The model's objective is to provide a link between local retail concentration and markups faced by consumers. We focus on how heterogeneous firms compete in an oligopolistic setup. Firms have market power in the local product markets in which they operate. To ensure tractability, we keep the modeling of demand as simple as possible. Demand for goods comes from a representative consumer, who supplies labor inelastically in each market and demands a national consumption good—a composite of all goods in the economy. The model closes with a perfectly competitive sector that aggregates individual goods from each market into the national consumption good.

F.1 The Model Economy

The model economy contains L locations, in each of them there are J products being transacted in local markets. Each location has N_{ℓ} retail firms that compete with one another in each good. Competition takes place at the location-product level. A perfectly competitive sector aggregates goods across firms for each product and location, aggregates products by location into location-specific retail goods, and aggregates each location's retail output into a final consumption good. A single representative consumer demands the final consumption good and supplies labor in each location.

F.1.1 Technology

A retailer *i* selling product *j* in location ℓ produces using only labor through a linear technology. $z_i^{j\ell}$ represents the productivity of the retailer:

$$y_i^{j\ell} = z_i^{j\ell} n_i^{j\ell}. \tag{F.1}$$

Labor is immobile across locations, but not products, so each location has a specific

wage, w_{ℓ} . Firms maximize profits for each market they operate in:

$$\pi_i^{j\ell} = p_i^{j\ell} y_i^{j\ell} - \lambda_i^{j\ell} y_i^{j\ell}, \qquad (F.2)$$

where $\lambda_i^{j\ell} = w_\ell / z_i^{j\ell}$ is the marginal cost of production.

The demand faced by the individual retailer comes from the aggregation sector that serves the consumer. Aggregation takes place in three levels. First, a local aggregator firm that combines the output of the N_{ℓ} retail firms selling product j in location ℓ . The firm operates competitively using the following technology:

$$y_j^{\ell} = \left(\sum_{i=1}^{N_{\ell}} \left(y_i^{j\ell}\right)^{\frac{\epsilon_j - 1}{\epsilon_j}}\right)^{\frac{\epsilon_j}{\epsilon_j - 1}}; \qquad \epsilon_j > 1.$$
(F.3)

Then, the combined product bundles, y_j^{ℓ} , are themselves aggregated into local retail output, y_{ℓ} , through the following technology:

$$y_{\ell} = \prod_{j=1}^{J} \left(y_{j}^{\ell} \right)^{\gamma_{j}^{\ell}}; \qquad \sum_{j=1}^{J} \gamma_{j}^{\ell} = 1,$$
 (F.4)

where γ_j^ℓ is the share of product j in retail sales in location ℓ

Finally, the national retail output is created by combining local output, y_{ℓ} , from the L locations in the country:

$$y = \prod_{\ell=1}^{L} (y_{\ell})^{\beta_{\ell}}; \qquad \sum_{\ell=1}^{L} \beta_{\ell} = 1,$$
 (F.5)

where β_{ℓ} corresponds to the share of location ℓ in national retail sales.

The aggregation process implies the following demand and prices:

$$y_{\ell} = \beta_{\ell} \frac{P}{p_{\ell}} \cdot y \qquad \qquad P = \prod_{\ell=1}^{L} \left(\frac{p_{\ell}}{\beta_{\ell}}\right)^{\beta_{\ell}}$$
(F.6)

$$y_j^{\ell} = \gamma_j^{\ell} \frac{p_{\ell}}{p_j^{\ell}} y_{\ell} \qquad \qquad p_{\ell} = \prod_{j=1}^J \left(\frac{p_j^{\ell}}{\gamma_j^{\ell}} \right)^{\gamma_j^{\ell}} \tag{F.7}$$

$$y_i^{j\ell} = \left(\frac{p_i^{j\ell}}{p_j^\ell}\right)^{-\epsilon_j} y_j^\ell \qquad \qquad p_j^\ell = \left(\sum_{i=1}^N \left(p_i^{j\ell}\right)^{1-\epsilon_j}\right)^{\frac{1}{1-\epsilon_j}} \tag{F.8}$$

F.1.2 Pricing to market

Firms compete directly in the sales of each product in a given location. We assume that firms are aware of the effect of their choices $\left(p_i^{j\ell}, y_i^{j\ell}\right)$ on the price and quantity of the product in the market they operate in $\left(p_j^{\ell}, y_j^{\ell}\right)$, but take as given the prices and quantities of other products in the same market, and of all products in other markets.

Firms choose either the price of their good $(p_i^{j\ell})$ of the quantity $(y_i^{j\ell})$ in a noncooperative fashion, taking as given the choices of other firms. We solve the pricing problem for Bertrand and Cournot competition (choosing prices or quantities respectively), as well as for the Dixit-Stiglitz monopolistic competition case, which serves as a useful framework.

The solution to the pricing problem is summarized in the following proposition taken from Grassi (2017):

Proposition 1. The optimal price of a firm takes the form: $p_i^{j\ell} = \mu_i^{j\ell} \lambda_i^{j\ell}$, where $\mu_i^{j\ell}$ is a firm-product-market specific markup that depends on the form of competition:

$$\mu_{i}^{j\ell} = \begin{cases} \frac{\epsilon_{j}}{\epsilon_{j}-1} & \text{if Dixit-Stiglitz monopolistic competition} \\ \frac{\epsilon_{j}-(\epsilon_{j}-1)s_{i}^{j\ell}}{\epsilon_{j}-1-(\epsilon_{j}-1)s_{i}^{j\ell}} & \text{if Bertrand competition} \\ \frac{\epsilon_{j}}{\epsilon_{j}-1-(\epsilon_{j}-1)s_{i}^{j\ell}} & \text{if Cournot competition} \end{cases}$$
(F.9)

and $s_i^{j\ell}$ is the sales share of the firm in the given product market:

$$s_i^{j\ell} = \frac{p_i^{j\ell} y_i^{j\ell}}{p_j^{\ell} y_j^{\ell}} = \left(\frac{p_i^{j\ell}}{p_j^{\ell}}\right)^{1-\epsilon_j} = \left(\frac{y_i^{j\ell}}{y_j^{\ell}}\right)^{\frac{\epsilon_j - 1}{\epsilon_j}}$$
(F.10)

We show details for the derivation in what follows.

Dixit-Stiglitz monopolistic competition The problem takes as given the product's price (p_j^{ℓ}) and aggregate demand (y_j^{ℓ}) . The objective is to maximize profits by choosing

the firm's price $\left(p_i^{j\ell}\right)$:

$$\max_{p_i^{j\ell}} p_i^{j\ell} y_i^{j\ell} - \lambda_i^{j\ell} y_i^{j\ell} \qquad \text{s.t. } y_i^{j\ell} = \left(\frac{p_i^{j\ell}}{p_j^\ell}\right)^{-\epsilon_j} y_j^\ell$$

Replacing the constraint:

$$\max_{p_i^{j\ell}} \left[\left(p_i^{j\ell} \right)^{1-\epsilon_j} - \lambda_i^{j\ell} \left(p_i^{j\ell} \right)^{-\epsilon_j} \right] \left(p_j^{\ell} \right)^{\epsilon_j} y_j^{\ell}$$

The first order condition is:

$$0 = (1 - \epsilon_j) \left(p_i^{j\ell} \right)^{-\epsilon_j} + \epsilon_j \lambda_i^{j\ell} \left(p_i^{j\ell} \right)^{-\epsilon_j - 1}$$
$$0 = (1 - \epsilon_j) p_i^{j\ell} + \epsilon_j \lambda_i^{j\ell}$$

Rearranging gives the result:

$$p_i^{j\ell} = \mu_i^{j\ell} \lambda_i^{j\ell} \qquad \mu_i^{j\ell} = \frac{\epsilon_j}{\epsilon_j - 1}$$

Bertrand competition The problem takes into account the effect of changes in the firm's own price on the product's price (p_j^{ℓ}) and aggregate demand (y_j^{ℓ}) . The objective is to maximize profits by choosing the firm's price $(p_i^{j\ell})$:

$$\max_{p_i^{j\ell}} p_i^{j\ell} y_i^{j\ell} - \lambda_i^{j\ell} y_i^{j\ell}$$
s.t. $y_i^{j\ell} = \left(\frac{p_i^{j\ell}}{p_j^\ell}\right)^{-\epsilon_j} y_j^\ell \qquad y_j^\ell = \gamma_j^\ell \frac{p_m y_\ell}{p_j^\ell} \qquad p_j^\ell = \left(\sum_{i=1}^N \left(p_i^{j\ell}\right)^{1-\epsilon_j}\right)^{\frac{1}{1-\epsilon_j}}$

Replacing the constraints:

$$\max_{p_i^{j\ell}} \left[\left(p_i^{j\ell} \right)^{1-\epsilon_j} - \lambda_i^{j\ell} \left(p_i^{j\ell} \right)^{-\epsilon_j} \right] \left(\sum_{i=1}^N \left(p_i^{j\ell} \right)^{1-\epsilon_j} \right)^{-1} \gamma_j^{\ell} p_\ell y_\ell$$

The first order condition is:

$$0 = \left[(1 - \epsilon_j) \left(p_i^{j\ell} \right)^{-\epsilon_j} + \epsilon_j \lambda_i^{j\ell} \left(p_i^{j\ell} \right)^{-\epsilon_j - 1} \right] \left(\sum_{i=1}^N \left(p_i^{j\ell} \right)^{1 - \epsilon_j} \right)^{-1} \\ - (1 - \epsilon_j) \left[\left(p_i^{j\ell} \right)^{1 - \epsilon_j} - \lambda_i^{j\ell} \left(p_i^{j\ell} \right)^{-\epsilon_j} \right] \left(\sum_{i=1}^N \left(p_i^{j\ell} \right)^{1 - \epsilon_j} \right)^{-2} \left(p_i^{j\ell} \right)^{-\epsilon_j} \\ 0 = \left[(1 - \epsilon_j) p_i^{j\ell} + \epsilon_j \lambda_i^{j\ell} \right] - (1 - \epsilon_j) \left[p_i^{j\ell} - \lambda_i^{j\ell} \right] \left(p_i^{j\ell} \right)^{1 - \epsilon_j} \left(p_j^{\ell} \right)^{\epsilon_j - 1} \\ 0 = \left[(1 - \epsilon_j) p_i^{j\ell} + \epsilon_j \lambda_i^{j\ell} \right] - (1 - \epsilon_j) \left[p_i^{j\ell} - \lambda_i^{j\ell} \right] s_i^{j\ell}$$

Rearranging gives the result:

$$p_i^{j\ell} = \mu_i^{j\ell} \lambda_i^{j\ell} \qquad \mu_i^{j\ell} = \frac{\epsilon_j - (\epsilon_j - 1) s_i^{j\ell}}{\epsilon_j - 1 - (\epsilon_j - 1) s_i^{j\ell}}$$

Cournot competition The problem takes into account the effect of changes in the firm's own price on the product's price (p_j^{ℓ}) and aggregate demand (y_j^{ℓ}) . The objective is to maximize profits by choosing the firm's quantity $(y_i^{j\ell})$:

$$\max_{y_i^{j\ell}} p_i^{j\ell} y_i^{j\ell} - \lambda_i^{j\ell} y_i^{j\ell}$$
s.t.
$$p_i^{j\ell} = \left(\frac{y_i^{j\ell}}{y_j^{\ell}}\right)^{\frac{-1}{\epsilon_j}} p_j^{\ell} \qquad p_j^{\ell} = \gamma_j^{\ell} \frac{p_\ell y_\ell}{y_j^{\ell}} \qquad y_j^{\ell} = \left(\sum_{i=1}^N \left(y_i^{j\ell}\right)^{\frac{\epsilon_j - 1}{\epsilon_j}}\right)^{\frac{\epsilon_j}{\epsilon_j - 1}}$$

Replacing the constraints:

$$\max_{y_i^{j\ell}} \left(y_i^{j\ell} \right)^{\frac{\epsilon_j - 1}{\epsilon_j}} \left(\sum_{i=1}^N \left(y_i^{j\ell} \right)^{\frac{\epsilon_j - 1}{\epsilon_j}} \right)^{-1} \gamma_j^{\ell} p_\ell y_\ell - \lambda_i^{j\ell} y_i^{j\ell}$$

The first order condition is:

$$\begin{split} 0 &= \frac{\epsilon_j - 1}{\epsilon_j} \left[\left(y_i^{j\ell} \right)^{\frac{-1}{\epsilon_j}} \left(y_j^{\ell} \right)^{\frac{1 - \epsilon_j}{\epsilon_j}} - \left(y_i^{j\ell} \right)^{2\frac{\epsilon_j - 1}{\epsilon_j} - 1} \left(y_j^{\ell} \right)^{2\frac{1 - \epsilon_j}{\epsilon_j}} \right] \gamma_j^{\ell} p_\ell y_\ell - \lambda_i^{j\ell} \\ 0 &= (\epsilon_j - 1) \left[1 - \left(\frac{y_i^{j\ell}}{y_j^{\ell}} \right)^{\frac{\epsilon_j - 1}{\epsilon_j}} \right] \left(\frac{y_i^{j\ell}}{y_j^{\ell}} \right)^{\frac{-1}{\epsilon_j}} \frac{\gamma_j^{\ell} p_\ell y_\ell}{y_j^{\ell}} - \epsilon_j \lambda_i^{j\ell} \\ 0 &= (\epsilon_j - 1) \left[1 - s_i^{j\ell} \right] p_i^{j\ell} - \epsilon_j \lambda_i^{j\ell} \end{split}$$

Rearranging gives the result:

$$p_i^{j\ell} = \mu_i^{j\ell} \lambda_i^{j\ell} \qquad \mu_i^{j\ell} = \frac{\epsilon_j}{\epsilon_j - 1 - (\epsilon_j - 1) \, s_i^{j\ell}}$$

F.1.3 Consumers

There is a representative consumer who has preferences over consumption of a national retail good, c. The consumer supplies labor inelastically in each location, with the local labor supply given by $\{n_{\ell}\}$.³⁸ The consumer receives income from profits and wages. The consumer's problem is:

$$\max_{\{c\}} u(c) = \frac{c^{1-\sigma}}{1-\sigma} \quad \text{s.t. } p \cdot c \le \sum_{\ell} n_{\ell} w_{\ell} + \Pi.$$
(F.11)

We normalize total labor supply, $n^S \equiv \sum_{\ell=1}^L n_\ell$, to one.

F.1.4 Equilibrium

The equilibrium of the model is standard and consists of a set of prices $\{P, \{p_\ell\}, \{p_j^\ell\}, \{p_i^{j\ell}\}\}$, wages $\{w_\ell\}$, outputs $\{y, \{y_\ell\}, \{y_j^\ell\}, \{y_i^{j\ell}\}\}$ and aggregate consumption demand, c, such that:

- 1. Aggregate prices and quantities satisfy F.6, F.7, and F.8.
- 2. Firm prices satisfy F.9, with the market share of each firm satisfying F.10.
- 3. Firm *i*'s labor demand is given by $n_i^{j\ell} = y_i^{j\ell}/y_i^{j\ell}$.
- 4. Wages are such that local labor markets clear, that is, for each ℓ :

$$n_{\ell} = \sum_{j=1}^{J} \sum_{i=1}^{N_{\ell}} n_i^{j\ell}$$

where $n_i^{j\ell} = y_i^{j\ell}/y_i^{j\ell}$ corresponds to firm *i*'s labor demand.

 38 In appendix F.4.2 we extend the model to include elastic labor supply.

F.2 Aggregating Markups

We now aggregate markups and productivity at the three levels of the economy (productlocation, location, national).

F.2.1 Product-Location Level

The objective is to define an average markup for product j in location $\ell(\mu_j^{\ell})$, as well as the average productivity of firms producing product j in location $\ell(z_j^{\ell})$.

Average Markup The average markup is given by the ratio between the price p_j^{ℓ} and product-market marginal cost λ_j^{ℓ} . Because of constant returns to scale λ_j^{ℓ} is also the average cost:

$$\lambda_j^\ell = \frac{\sum_i \lambda_i^{j\ell} y_i^{j\ell}}{y_j^\ell} = \sum_{i=1}^N \lambda_i^{j\ell} \frac{y_i^{j\ell}}{y_j^\ell}$$

then the average markup is:

$$\mu_{j}^{\ell} = \frac{p_{j}^{\ell}}{\lambda_{j}^{\ell}} = \left[\sum_{i=1}^{N} \lambda_{i}^{j\ell} \frac{y_{i}^{j\ell}}{p_{j}^{\ell} y_{j}^{\ell}}\right]^{-1} = \left[\sum_{i=1}^{N} \left(\frac{\lambda_{i}^{j\ell}}{p_{i}^{j\ell}}\right) \left(\frac{p_{i}^{j\ell} y_{i}^{j\ell}}{p_{j}^{\ell} y_{j}^{\ell}}\right)\right]^{-1} = \left[\sum_{i=1}^{N} \left(\mu_{i}^{j\ell}\right)^{-1} s_{i}^{j\ell}\right]^{-1},$$

that is, a harmonic mean of individual markups, weighted by sales shares.

It is possible to further solve for the markup using the solution to the pricing problem above. The result is taken from Proposition 4 in Grassi (2017):

Proposition 2. The average markup for product *j* in market *m* is:

$$\mu_{j}^{\ell} = \begin{cases} \frac{\epsilon_{j}}{\epsilon_{j}-1} & \text{if Dixit-Stiglitz monopolistic competition} \\ \frac{\epsilon_{j}}{\epsilon_{j}-1} \left[\frac{1}{\epsilon_{j}-1} \sum_{k=2}^{\infty} \left(\frac{\epsilon_{j}-1}{\epsilon_{j}} \right)^{k-1} \left(HK_{j}^{\ell}\left(k\right) \right)^{k} \right]^{-1} & \text{if Bertrand competition} \\ \frac{\epsilon_{j}}{\epsilon_{j}-1} \left[1 - HHI_{j}^{\ell} \right]^{-1} & \text{if Cournot competition} \end{cases}$$

where $HK_{j}^{\ell}(k)$ is the Hanna & Kay (1977) concentration index of order k:

$$HK_{j}^{\ell}\left(k\right) = \left[\sum_{i=1}^{N} \left(s_{i}^{j\ell}\right)^{k}\right]^{\frac{1}{k}}$$

1

and
$$HHI_{j}^{\ell} = HK_{j}^{\ell}(2)^{2} = \sum_{i} \left(s_{i}^{j\ell}\right)^{2}$$
 is the Herfindahl-Hirschman Index.

Average Productivity The average product is also obtained from the marginal (average) cost:

$$\lambda_{j}^{\ell} = \sum_{i=1}^{N} \lambda_{i}^{j\ell} \frac{y_{i}^{j\ell}}{y_{j}^{\ell}} = \left[\sum_{i=1}^{N} \left(z_{i}^{j\ell}\right)^{-1} \frac{y_{i}^{j\ell}}{y_{j}^{\ell}}\right] w_{\ell}$$

which implies:

$$z_{j}^{\ell} = \left[\sum_{i=1}^{N} \left(z_{i}^{j\ell}\right)^{-1} \frac{y_{i}^{j\ell}}{y_{j}^{\ell}}\right]^{-1},$$

an output-weighted harmonic mean of productivities.

F.2.2 Local market and national level

Markups and productivities can be aggregated again at the market level (aggregating across products) by defining first the market's marginal (average) cost:

$$\lambda_\ell = \frac{\sum \lambda_j^\ell y_j^\ell}{y_\ell}$$

For markups this implies:

$$\mu_{\ell} = \frac{p_{\ell}}{\lambda_{\ell}} = \left[\sum_{j=1}^{J} \left(\mu_{j}^{\ell}\right)^{-1} s_{j}^{\ell}\right]^{-1} = \left[\sum_{j=1}^{J} \left(\mu_{j}^{\ell}\right)^{-1} \gamma_{j}^{\ell}\right]^{-1}$$

For productivity:

$$z_{\ell} = \frac{w_{\ell}}{\lambda_{\ell}} = \left[\sum_{j=1}^{J} \left(z_j^{\ell}\right)^{-1} \frac{y_j^{\ell}}{y_{\ell}}\right]^{-1}$$

The same procedure gives the markup for the national level:

$$\mu = \left[\sum_{\ell=1}^{L} \left(\mu_{\ell}\right)^{-1} \beta_{\ell}\right]^{-1}$$

We define the productivity at the national level as the harmonic mean of local productivities weighted by output shares:

$$z \equiv \left[\sum_{\ell=1}^{L} \left(z_{\ell}\right)^{-1} \frac{y_{\ell}}{y}\right]^{-1}$$

This expression does not follow as the others because the cost of production (w_{ℓ}) differs across markets.

Multi-product/Multi-market firm Note that the equations above also apply to firms that sell various products and operate in various markets, modifying the sums to account only for the firm's products and markets.

F.2.3 Product aggregation

We also compute the average markup of a product across markets. This measure is relevant because it can be obtained directly from the data. We define the average markup

$$\mu_j \equiv \frac{\sum_{\ell=1}^L p_j^\ell y_j^\ell}{\sum_{\ell=1}^L w_\ell l_j^\ell}$$

as the ratio between product j's total sales and total labor costs of the product across markets ($\ell = 1, \ldots, L$). The average markup is given in the model by:

$$\mu_{j} \equiv \frac{\sum_{\ell=1}^{L} p_{j}^{\ell} y_{j}^{\ell}}{\sum_{\ell=1}^{L} w_{\ell} l_{j}^{\ell}} = \frac{\sum_{\ell=1}^{L} p_{j}^{\ell} y_{j}^{\ell}}{\sum_{\ell=1}^{L} \frac{\lambda_{j}^{\ell}}{p_{j}^{\ell}} p_{j}^{\ell} y_{j}^{\ell}} = \left[\sum_{\ell=1}^{L} \left(\mu_{j}^{\ell}\right)^{-1} \theta_{j}^{\ell}\right]^{-1},$$

a harmonic mean of market level markups for product j, weighted by the share of product j sales in market ℓ captured by $\theta_j^{\ell} \equiv \frac{p_j^{\ell} y_j^{\ell}}{\sum_{\ell=1}^L p_j^{\ell} y_j^{\ell}} = \frac{\gamma_j^{\ell} \beta_{\ell}}{\sum_{\ell=1}^L \gamma_j^{\ell} \beta_{\ell}}.$

Using the result in Proposition 2 it is possible to express the product markup in terms of market concentration. For the case of Cournot competition it gives:

$$\mu_j = \left[\sum_{\ell=1}^L \left(\frac{\epsilon_j^\ell}{\epsilon_j^\ell - 1}\right)^{-1} \left[1 - \mathrm{HHI}_j^\ell\right] \theta_j^\ell\right]^{-1}$$

If the elasticity of substitution across varieties of good j is common across markets the expression simplifies to:

$$\mu_j = \frac{\epsilon_j}{\epsilon_j - 1} \left[1 - \mathrm{HHI}_j \right]^{-1},$$

where $\text{HHI}_j \equiv \sum_{\ell=1}^{L} \text{HHI}_j^{\ell} \theta_j^{\ell}$ is the sales weighted Herfindahl-Hirschman Index of product j across market.

F.3 Estimation Steps

We estimate the model using product level data from the Census of Retail Trade and the Annual Retail Trade Survey. This allows us to discuss how conditions in the average U.S. market has changed. To accomplish this we use the estimates of local concentration from section 4.2 and data on markups, prices, output, and labor supply. As in the empirical analysis of sections 3 and 4, we define markets in the model as pairs of a commuting zone and one of the product categories described in Table C.1.

The Cobb-Douglas parameters, β_{ℓ} and γ_{j}^{ℓ} , are obtained from the Census of Retail Trade as the share of spending on each product in a commuting zone. The estimation of the elasticity of substitution parameters consists on matching the product level markup from the ARTS given the product's average local concentration. From equation (7) we get:

$$\hat{\epsilon}_j = \frac{\hat{\mu}_j \left[1 - \sum_{\ell} s_{\ell}^j H H I_j^{\ell} \right]}{\hat{\mu}_j \left[1 - \sum_{\ell} s_{\ell}^j H H I_j^{\ell} \right] - 1}$$
(F.12)

where $\hat{\mu}_j = \frac{\text{Sales}_j}{\text{Cost of Goods Sold}_j}$ is the gross markup for product j. We use 2007 ARTS data for the estimation of the elasticity of substitution, matching all products' markups in that year by construction. Using our estimate of the elasticity of substitution parameters and the measured series for the product-level HHI we construct the series of markups implied by the model through equation (7).

We also define implicit price and quantity indexes for each product such that they are consistent with total sales of the product across markets:

$$P_j Y_j = \sum_{\ell} p_j^{\ell} y_j^{\ell} \tag{F.13}$$

Given the quantity index we define the average (marginal) cost of goods for a product, λ_j , as the output-weighted average of the individual market costs:

$$\lambda_j \equiv \sum_{\ell} \lambda_j^{\ell} \frac{y_j^{\ell}}{Y_j}.$$
 (F.14)

Note that the average cost satisfies the following pricing equation at the product level:

$$P_j = \mu_j \lambda_j. \tag{F.15}$$

Finally, we can aggregate our product-level results to obtain a measure of the average retail cost and markup. The average cost is defined, as before, as the output-weighted average of the individual product costs:

$$\lambda \equiv \sum_{j} \lambda_{j} \frac{y_{j}}{Y},\tag{F.16}$$

where Y is a quantity index for the retail sector. The average markup is defined as the ratio of total sales to cost:

$$\mu \equiv \frac{\sum_{j} P_{j} Y_{j}}{\sum_{j} \lambda_{j} Y_{j}} = \frac{\sum_{j} P_{j} Y_{j}}{\sum_{j} \frac{\lambda_{j}}{P_{j}} P_{j} Y_{j}} = \left[\sum_{j} \left(\mu_{j}\right)^{-1} s_{j}\right]^{-1}, \qquad (F.17)$$

where s_j is the expenditure share of product j. As before this measure of markup satisfies the pricing equation at the national level:

$$P = \mu\lambda, \tag{F.18}$$

where P is a retail price index satisfying:

$$PY = \sum_{j} P_{j}Y_{j}.$$
 (F.19)

F.3.1 Comparing Results Across Time

To compare our model's cross-sectional results across time we choose normalizations for prices that make aggregate numbers consistent with published statistics.³⁹ We use data on the change of retail good prices from the Price Indexes for Personal Consumption, from the U.S. Bureau of Economic Analysis (2020). These data provides us with series for the price index of each good category.⁴⁰ Each price index defines the inflation of prices in its

³⁹The level of the aggregate price does not affect relative prices, output, or markups in the model.

⁴⁰The price index for some product categories is not directly provided by the BEA data. In these cases we construct the category's index from individual product's series in the same way as we construct the aggregate retail index from the product category indexes.

respective category. We normalize the index so that $P_j^{1987} = 1$ for all product categories $j = 1, \ldots, J$. The level of the price index in year t reflects the cumulative (gross) inflation of prices in the product category.

We aggregate the individual category price indexes following the same procedure as the BEA. This procedure defines the aggregate index as an expenditure share weighted geometric average of the categories' indexes, the same definition as in our model (see equation F.6). Since the level of the individual indexes is arbitrary and only allows for direct comparisons across time and not products, we construct the aggregate index indirectly by computing its change over time:

$$\frac{P_t}{P_{t-1}} = \prod_{j=1}^J \left(\frac{P_j^t}{P_j^{t-1}}\right)^{s_j^t}.$$
 (F.20)

We normalize the aggregate index so that $P_{1992} = 1$, and obtain the level in subsequent periods by concatenating the changes obtained in equation (F.20). As before the index provides the cumulative (gross) inflation in retail prices since 1992.

Finally, we deflate our retail price index by overall inflation. Without this adjustment the index reflects not only changes in retail prices, but also trends in overall inflation due to monetary or technological phenomena that are outside of the scope of the model. From these data we find retail prices decreased 35 percent relative to overall inflation. We use aggregate price index we obtain and the average retail markup (equation F.17) to compute the value of the average marginal cost λ , implied by equation (F.18).

F.4 Extensions

F.4.1 Marginal Costs Functional Form

In the baseline model production at a retail uses only labor as an input. In this section we evaluate how our setup maps to the case where the firms uses an arbitrary constantreturns-to-scale technology that uses labor and other materials.

Consider the problem of retail firms that use multiple inputs $\{x_k\}_{k=1}^{K}$ in addition to

labor to produce:

$$y_i^{j\ell} = \tilde{z}_i^{j\ell} F\left(x_1, \dots, x_K, n_i^{j\ell}\right), \qquad (F.21)$$

where the function F is strictly concave, twice continuously differentiable, and has constant returns to scale. Letting the prices of inputs be $\{\tilde{p}_k\}_{k=1}^K$ and \tilde{w}_ℓ respectively, we know from the firm's optimality condition that:

$$\tilde{z}_i^{j\ell} F_k\left(\frac{x_1}{n_i^{j\ell}}, \dots, \frac{x_K}{n_i^{j\ell}}, 1\right) = \tilde{p}_k \tag{F.22}$$

recalling that, because of Euler's theorem, F_k is homogeneous of degree zero for every k.

The equations defined by (F.22) define a square system in the ratio ratio of each input x_k to labor. The system has a solution that gives the ratios in terms of parameters:

$$\frac{x_k}{n_i^{j\ell}} = g_k\left(\tilde{z}_i^{j\ell}, \tilde{p}_1, \dots, \tilde{p}_K\right)$$
(F.23)

The existence of a solution follows from the inverse function theorem applied to the function $\nabla_x F : \mathbb{R}_{++}^K \to \mathbb{R}_{++}^K$, where the operator ∇_x gives the first derivatives of F with respect to the variables $\{x_k\}_{k=1}^K$. Note that the Jacobian of ∇F is given by the first K rows and columns of the Hessian of F, which is negative definite for all interior points by the strict concavity of F. The negative definiteness of the Jacobian ensures the invertibility of $\nabla_x F$.

Given the system's solution we express the production function in terms of labor alone:

$$y_i^{j\ell} = \tilde{z}_i^{j\ell} F\left(\frac{x_1}{n_i^{j\ell}}, \dots, \frac{x_K}{n_i^{j\ell}}, 1\right) n_i^{j\ell} = z_i^{j\ell} n_i^{j\ell}$$

where we define the effective productivity of labor as $z_i^{j\ell} \equiv \tilde{z}_i^{j\ell} F(x_1/n_i^{j\ell}, \dots, x_K/n_i^{j\ell}, 1)$ with the ratios $x_k/n_i^{j\ell}$ given as in (F.23). Thus, z_i^j is a function of productivity $\tilde{z}_i^{j\ell}$ and the price of the other inputs. This is the production function we use in the main model.

Finally, the cost of labor must take into account that other inputs react to changes in labor according to (F.23). Then, the cost of the firm is given by:

$$\sum_{k=1}^{K} \tilde{p}_k x_k + \tilde{w}_\ell n_i^{j\ell} = \left(\sum_{k=1}^{K} \tilde{p}_k \frac{x_k}{n_i^{j\ell}} + \tilde{w}_\ell\right) n_i^{j\ell} = w_\ell n_i^{j\ell}$$

where $w_{\ell} n_i^{j\ell}$ represents the cost of goods sold, and w_{ℓ} is not directly the wage, but a measure

of costs that takes into account the price of other inputs and the change in their demand in response to changes in the firm's labor demand.

F.4.2 Elastic Labor Supply

In this section we outline a version of the model where consumers have preferences over national consumption (c) and leisure/labor in each location: $u(c, n_1, \ldots, n_L)$. This setup does not affect any of the results in the paper as all results using the markup equation go through unchanged.

We consider a utility function that is separable in consumption and labor:

$$u(c, \{n_{\ell}\}) = \frac{c^{1-\sigma}}{1-\sigma} - \chi \sum_{\ell=1}^{L} \frac{(n_{\ell})^{1+\frac{1}{\phi}}}{1+\frac{1}{\phi}} \quad \text{and} \quad \chi c^{\sigma} (n_{\ell})^{\frac{1}{\phi}} = \frac{w_{\ell}}{P}$$

 ϕ corresponds to the Frisch elasticity of labor supply. σ is the curvature of utility in consumption.

The first order conditions of the consumer imply:

$$\frac{u_{n_{\ell}}(c, \{n_{\ell}\})}{u_{c}(c, \{n_{\ell}\})} = \frac{w_{\ell}}{P}.$$

This governs how total labor supply reacts to changes in prices and changes in markups. These results affect how productivity and output respond to changes in prices.

F.4.3 Uniform prices across locations

Consider now the problem of firm *i* that sales product *j* across various markets $\ell \in \mathcal{L}_i$. There are three options for pricing: pricing to market, ignoring linkages of demand across markets, pricing to market incorporating linkages of demand, uniform pricing. We deal with them in turn.

The first price option (pricing to market, ignoring effects on demand across markets) gives the same solution as above, and the aggregation is also the same. The second option would require the firm to take into account the effect on the demand for groceries in New York of a price change in groceries in Minneapolis. We consider this to be implausible, and

the effect to be likely very small (even if firms are taking into account). Thus we think this case is well approximated by our baseline case above. The final option is uniform pricing, which we solve for below.

The problem of the firm is:

$$\max_{p_i^j} \sum_{\ell \in \mathcal{L}_i} \left[p_i^j y_i^{j\ell} - \lambda_i^{j\ell} y_i^{j\ell} \right]$$

s.t. $y_i^{j\ell} = \left(\frac{p_i^j}{p_j^\ell} \right)^{-\epsilon_j} y_j^\ell \qquad y_j^\ell = \gamma_j^\ell \frac{p_\ell y_\ell}{p_j^\ell} \qquad p_j^\ell = \left(\sum_{i=1}^N \left(p_i^{j\ell} \right)^{1-\epsilon_j} \right)^{\frac{1}{1-\epsilon_j}}$

Replacing the constraints:

$$\max_{p_i^j} \sum_{\ell \in \mathcal{L}_i} \left[\left(p_i^j \right)^{1-\epsilon_j} - \lambda_i^{j\ell} \left(p_i^j \right)^{-\epsilon_j} \right] \left(\sum_{i=1}^N \left(p_i^{j\ell} \right)^{1-\epsilon_j} \right)^{-1} \gamma_j^{\ell} p_\ell y_\ell$$

The first order condition is:

$$0 = \sum_{\ell \in \mathcal{L}_i} \left[\left[\left(1 - \epsilon_j \right) p_i^j + \epsilon_j \lambda_i^{j\ell} \right] \frac{y_i^{j\ell}}{p_i^j} - \left(1 - \epsilon_j \right) \left[p_i^j - \lambda_i^{j\ell} \right] s_i^{j\ell} \frac{y_i^{j\ell}}{p_i^j} \right]$$
$$0 = \sum_{\ell \in \mathcal{L}_i} \left[-\left(\epsilon_j - 1 \right) \left(1 - s_i^{j\ell} \right) y_i^{j\ell} p_i^j + \left(\epsilon_j - \left(\epsilon_j - 1 \right) s_i^{j\ell} \right) \lambda_i^{j\ell} y_i^{j\ell} \right]$$

Rearranging:

$$p_i^j = \frac{\sum_{\ell} \left(\epsilon_j - (\epsilon_j - 1) s_i^{j\ell}\right) \lambda_i^{j\ell} y_i^{j\ell}}{\sum_{\ell} (\epsilon_j - 1) \left(1 - s_i^{j\ell}\right) y_i^{j\ell}}$$

If marginal cost is constant across markets then we define the markup :

$$p_i^j = \mu_i^j \lambda_i^j \qquad \mu_i^j = \frac{\sum_{\ell} \left(\epsilon_j - (\epsilon_j - 1) s_i^{j\ell}\right) y_i^{j\ell}}{\sum_{\ell} \left(\epsilon_j - 1\right) \left(1 - s_i^{j\ell}\right) y_i^{j\ell}}$$

The firm's markup reflects its market power across different markets, captured by the firm's output-weighted average share, \hat{s}_i^j . Define $\hat{y}_i^{j\ell} = \frac{y_i^{j\ell}}{\sum_{\ell} y_i^{j\ell}}$, then:

$$\mu_{i}^{j} = \frac{\sum_{\ell} \left(\epsilon_{j} - (\epsilon_{j} - 1) s_{i}^{j\ell}\right) \hat{y}_{i}^{j\ell}}{\sum_{\ell} \left(\epsilon_{j} - 1\right) \left(1 - s_{i}^{j\ell}\right) \hat{y}_{i}^{j\ell}} = \frac{\epsilon_{j} - (\epsilon_{j} - 1) \sum_{\ell} s_{i}^{j\ell} \hat{y}_{i}^{j\ell}}{(\epsilon_{j} - 1) \left(1 - \sum_{\ell} s_{i}^{j\ell} \hat{y}_{i}^{j\ell}\right)} = \frac{\epsilon_{j} - (\epsilon_{j} - 1) \hat{s}_{i}^{j}}{(\epsilon_{j} - 1) \left(1 - \hat{s}_{i}^{j}\right)}$$

The firm's uniform markup is lower than the average markup if the firm chooses prices in

each market separately. To see this, define the firm's average price in product j such that:

$$p_i^j y_i^j = \sum_{\ell} p_i^{j\ell} y_i^{j\ell},$$

where $y_i^j \equiv \sum_{\ell} y_i^{j\ell}$. It follows that $p_i^j = \sum_{\ell} p_i^{j\ell} \hat{y}_i^{j\ell}$. The average markup would then be:

$$\mu_i \equiv \frac{p_i^j}{\lambda_i^j} = \sum_{\ell} \frac{p_i^{j\ell}}{\lambda_i^j} \hat{y}_i^{j\ell} = \sum_{\ell} \mu_i^{j\ell} \hat{y}_i^{j\ell},$$

which is the output-weighted average of the individual market markups. This average is higher than the uniform markup. The result follows from Jensen's inequality as the Bertrand markup is convex in the firm's sales share.